Firm-Level Shocks and Labor Adjustments*

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Abstract

We analyze how firms adjust their labor in response to idiosyncratic shifts in their production functions and firm-level demand curves using unique data on Swedish manufacturing firms. We show that the adjustment to permanent firm-level demand shocks is substantial, rapid and unconstrained. The choice of adjustment margin depends on the sign of the shock: Firms adjust through increased hires if these shocks are positive and through increased separations if the shocks are negative. In contrast, both transitory demand shocks and shocks to physical productivity have only modest effects on firm-level employment decisions, despite being important determinants of other firm-level fundamentals.

Keywords: Technology, Demand, Job Flows, Worker Flows

JEL classifications: J23, J63, C33

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1 Introduction

About one in every five jobs are either created or destroyed every year (Davis, Faberman, and Haltiwanger, 2006). The bulk of this firm-level labor adjustment is truly idiosyncratic as firms operating in the same sector and area shrink and grow side-by-side. Hence, jobs are rapidly created and destroyed, even in sectors with stable net employment. Following the seminal work of Davis, Haltiwanger and Schuh (1996), the importance and magnitude of these labor flows has been documented for a large number of countries.\(^1\) However, while the empirical regularities of job and worker flows have been abundantly documented, little is known about how job and worker flows respond to structural firm-level shocks.\(^2\)

This paper presents novel evidence on how employment adjust through hires and separations when firms are hit by shocks that alter their positions in the performance distribution. We identify the two types of fundamental shocks highlighted by Foster, Haltiwanger, and Syverson (2008); Technology shocks shifting the firm-level physical production function (i.e., the ability to produce at a given level of inputs) and Demand shocks shifting the firm-level demand curve (i.e., the ability to sell at a given price).\(^3\)

We focus on the effects of idiosyncratic shocks, and thus concentrate on employment adjustments in a stable market environment, effectively abstracting from feedback effects through changes in market wages or aggregate unemployment. Moreover, we focus on permanent shocks and show that the distinction relative to transitory shocks is crucial, since permanent shocks are the key drivers of employment adjustments. Our empirical analysis relies on a unique data base that links measures of firm-level input, output, and prices to individual worker-flow data for Swedish manufacturing firms.

The analysis adds to a vibrant empirical literature, surveyed in Syverson (2011), that documents the distinct impacts of firm-level technology and demand shocks on productivity and other firm-level outcomes. Most notably, Foster et al. (2008) shows

\(^1\)See Davis, Faberman, and Haltiwanger (2012) for an overview. For evidence from Sweden, which is the empirical subject of this paper, see Andersson (2003).

\(^2\)A small macro-oriented literature aims to identify the employment responses to technology-driven changes in firm-level productivity, see e.g., Carlsson and Smedsaaas (2007) and Marchetti and Nucci (2005). The macro literature also contains a number of related studies, e.g., Gali (1999) and Michelacci and Lopez-Salido (2007), the latter of which distinguished between neutral technology shocks and investment-specific technology shocks and derived the consequences for job reallocation.

\(^3\)Importantly, these shocks are defined according to their effects on firm-level optimization, not according to their origins.
that firm closures are driven primarily by changes in idiosyncratic demand and only to a lesser extent by changes in idiosyncratic physical productivity. Recent evidence in Foster, Haltiwanger, and Syverson (2012) suggests that the growth of young firms in the US is due to a shrinking product-demand gap relative to incumbents. Pozzi and Schivardi (2015), who uses Italian data to analyze how technology and demand affect firm output, show that firm-level technology shocks have a surprisingly low impact on firm growth and that demand shocks are at least as important. In addition, Carlsson, Messina, and Nordström-Skans (2014) shows that firm-level technology shocks affect workers’ wages, using Swedish data.

This paper is, however, the first to focus on how firm-level technology and demand shocks affect firms’ labor adjustments through hires and separations in response to shocks of different nature, signs and magnitudes, a question that speaks to a huge body of theoretical research regarding the relationship between firm-level revenue productivity and labor adjustments (Bentolila and Bertola, 1990; Davis and Haltiwanger, 1992; Hopenhayn and Rogerson, 1993; Mortensen and Pissarides, 1994; and more recently Cahuc, Postel-Vinay, and Robin, 2006; and Lise, Meghir, and Robin, 2013). The focus of this paper is to disentangle the separate roles in labor adjustments of two fundamental drivers of firm-level revenue productivity fluctuations: demand and technology shocks.

As most previous empirical studies of firm-level shocks, our analysis departs from a stylized model of monopolistically competitive firms. The model motivates a set of restrictions on the long-run relationship between firm-level fundamentals and shocks. In the spirit of Franco and Philippon (2007), we then impose these long-run restrictions in a structural vector autoregression (SVAR) setting to filter out our empirical measures of permanent idiosyncratic demand and technology shocks. This allows us to derive the permanent shocks in a unified framework without imposing any restrictions on the firms’ short-run behavior.

The most important restriction we rely on is instead the notion that the physical gross Solow residual is independent of all shocks except the technology shock in the long run. To take the analysis to the data, we benefit from a firm-specific price index.

\footnote{Demand shocks appear to have a non-trivial transitory component which we remove in the main analysis and then study separately. In contrast, the bulk of the (physical) technology shocks are persistent enough to emerge as permanent shocks from our SVAR filter. This is consistent with Carlsson, Messina, and Nordström-Skans (2014) who, when estimating an AR(1) process for the level of technology using Swedish data similar to ours, find a persistence estimate as high as 0.88. Eslava et al. (2004) find an even higher persistence of 0.92 for Colombia.}
Using a strategy similar to Eslava et al. (2004), Carlsson, Messina, and Nordström-Skans (2014) and Smeets and Warzynski (2013), we deflate the (nominal) firm-level output series with firm-level price indices to derive measures of firm-level real output volumes. Importantly, the fact that we filter out the technology shocks using long-run restrictions implies that other shocks, or changes in factor utilization, or inventories, are allowed to have a transitory impact on the physical Solow residual without affecting the measured technology shocks.

Our model also allows us to derive sufficient restrictions to identify permanent demand shocks, again without imposing any restrictions on the nature of short-run shocks or dynamics. Since we use data from a small, open economy, our system also explicitly allows for shocks to factor prices.\footnote{In addition, the system allows for a (transitory) residual shock component to soak up any remaining short-run dynamics, including mean-reverting shocks to purely idiosyncratic factor prices.}

Although our modelling assumptions are very similar to the single-equation approach taken by previous research, where the demand shocks are calculated as residuals from output-price relationships using an estimated demand elasticity, the SVAR has the advantage of not imposing any structure or restrictions on the firms’ adjustments in the short run. It also provides us with results that are robust to transitory measurement errors and missmeasurement in the demand elasticity. A specific benefit we get from applying standard time-series econometrics tools is that they produce measures of shocks with known time-series properties in terms of persistence; properties which we show are of particular importance when studying labor adjustments. The strategy also allows us to account for confounding movements in factor prices, an issue which is likely to be of special importance for our open economy setting.

When implementing the SVAR, we deviate from standard time-series applications such as Blanchard and Quah (1989) and Franco and Philippon (2007). Because we have access to a wide panel of firms, we estimate the reduced-form equations using dynamic panel data methods building on Arellano and Bond (1991). This allows us to estimate both the parameters and the covariance matrix of the error terms with considerable precision, thereby avoiding standard macro-data concerns regarding the practical implementation of SVARs.

Before moving to the main analysis, we corroborate the interpretation of the idiosyncratic firm-level technology and demand shocks by showing that prices and output respond as theorized: Idiosyncratic output increases in response to positive shocks.
to both demand and technology. But firm-level prices decrease only in response to firm-level technology shocks, whereas they remain largely unaffected when demand shifts.

Turning to our key research questions, we start by showing that, despite being crucial for both firm-level prices and output, firm-level technology shocks have a relatively limited effect on labor inputs. In contrast, we find that product demand is a key driving force behind firm-level labor adjustments. An idiosyncratic demand shock of 1 standard deviation increases employment by 6 percent, whereas the corresponding number for technology shocks is 0.5 percent. Most of this adjustment takes place within a year. These results are robust to a wide range of variations in measures and specifications. We also show that the data seem to ask for a model where price responses to technology shocks are muted by non-constant demand elasticities, which we can allow for without violating the identifying assumptions.

We then use the product demand shocks as an instrument to uncover the causal component of the relationship between job flows and worker flows. This analysis builds on the seminal work of Abowd, Corbel, and Kramarz (1999) and Davis, Faberman, and Haltiwanger (2012) who provide descriptive studies of job flows and worker flows, decomposed into positive and negative changes using data from France and the United States, respectively. In contrast to these decomposition exercises, we analyze hires and separations in response to net employment changes driven by a well-identified and empirically relevant shock: permanent shifts in firms’ product demand schedules. This allows us, for the first time, to provide an analysis that removes the potential impact of exogenous variations in worker flows (e.g., any type of worker-induced separation) which can create endogenous responses in the number of jobs, particularly in small firms.

Our findings show that the employment adjustment induced by permanent demand shocks is both rapid and symmetric across hires and separations. On average, firms adjust employment almost as much through changes in the separation rate as through changes in the hiring rate. Although we find that the average firm reduces hires in response to negative shocks, it also continues to recruit workers even when

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6 The employment elasticity to technology shocks is 0.05 (or 0.14 if assuming decreasing returns to scale) which is very close to what Pozzi and Schivardi (2015) found for Italy (0.08) using a static single-equation approach. The demand shock responses are, however, much larger in our case (0.39 on elasticity form).

7 We further show that we can match estimated responses of output, prices and employment much better if we allow for endogenous demand elasticities.
forced to reduce employment substantially. Thus, the firms are far from exploiting the full potential of downsizing through reduced hires.\textsuperscript{8} The results thus imply that both hireings and separations should be treated as endogenous when modelling labor adjustments at the firm level. We also show that, in the face of negative shocks, only half of the separations are related to short-tenured workers.

Overall, the speed of adjustment, the symmetry between hires and separations as adjustment margins, the rapid separation of long-tenured workers, and the continued recruitment of workers in the face of negative shocks jointly suggest that firms facing permanent idiosyncratic demand shocks do adjust their labor input flexibly. In contrast, we show that the firms’ responses to transitory demand shocks are heavily muted. The results thus suggest that firms hoard labor and refrain from hiring when hit by transitory disturbances, but release and hire workers rapidly when hit by permanent changes in their product demand. This pattern may well be welfare-enhancing in the presence of uninsurable labor market risk (Bertola, 2004)\textsuperscript{9}

The paper is organized as follows: Section 2 outlines a simple model that motivates the long-run restrictions needed to extract our permanent demand and technology shocks. Section 3 introduces the main characteristics of the firm-level data used in the analysis and discusses the empirical implementation of the SVAR and the validation of the shocks. Section 4 reports the main results, distinguishing employment, hiring, and separation margins in response to technology and demand shocks. Section 5 presents extensions of the basic analysis, including a discussion of (i) the role of worker heterogeneity, and (ii) how transitory demand shocks affect employment adjustment. Finally, section 6 summarizes our results and findings.

\textsuperscript{8}These results thus concur with the descriptive picture provided by Davis, Faberman, and Haltiwanger (2012) for the US, but differ from Abowd, Corbel, and Kramarz (1999) who documents that employment reductions in French firms primarily are associated with reduced hiring rates.

\textsuperscript{9}See also Guiso, Schivardi, and Pistaferri (2005), who show that firms insure workers’ wages relative to transitory shocks to value added, but not to permanent shocks.
2 Model and Empirical Strategy

2.1 Shocks to Idiosyncratic Production Functions and Demand Curves

In this section, we derive a stylized model of monopolistically competitive firms. The model focuses on two key exogenous idiosyncratic driving forces to the firm’s relative performance: technology shocks affecting the firm’s physical productivity and demand shocks affecting the firm’s ability to sell to its products at a given price. The purpose of the paper is to analyze how these two disturbances affect firms’ hiring and separation policies. The model, functional form assumptions, and statistical properties of the shocks are deliberately stylized, imposing the minimum amount of structure needed to identify these two structural shocks using VAR techniques. In our empirical application, we do not impose the full set of structural assumptions which would be needed to identify the deep structural parameters of the model. Instead, we use a less restrictive approach, which only relies on a set of long-run neutrality restrictions between shocks and different variables implied by a stylized theoretical model.\(^\text{10}\)

The key distinction between our definitions of technology shocks and demand shocks lies in how the shock affects the producing firm, not in the origin of the shock. We therefore refrain from modeling the origins. This approach, which is consistent with the existing (micro) literature (such as Foster et al., 2008, and Syverson, 2011), implies that we do not distinguish between shifts in the firm-specific demand curve that arise from changing preferences among final consumers, those that arise from increased demand among downstream firms, and those that arise from quality changes that increase product demand at a given price.\(^\text{11}\)

To identify firm-level structural shocks, we need to make assumptions about the technology and market conditions faced by the firm. Our setup follows Eslava et al. (2004) and Foster et al. (2008, 2012) closely, by using a first-order approximation of

\(^{10}\)As we show, different representations of the demand structure give different mappings between empirical results and key structural parameters, while delivering unchanged long-run restrictions and thus unchanged findings in terms of labor-adjustment responses to the shocks.

\(^{11}\)Franco and Philippon (2007) label these shocks as shocks to market shares, and model them formally as preference shocks. Note that the firm-level price index we use is based on unit prices for very detailed product codes (8/9-digit Harmonized System/Combined Nomenclature codes), which limits the scope for quality changes to be the key component in our demand shock. However, it is straightforward to show that if we added a quality shock to the system developed below (through a wedge between the measured firm-level price, based on unit values, and the quality-adjusted price), it would enter the system symmetrically to the demand shock.
both production technologies and product market demand and by modeling the key technology and demand shocks as neutral shifters of the production function and the demand curve, respectively. Following these papers, the firm-level production function is approximated by:

$$Y_{jt} = A_{jt}N_{jt}^{\alpha}K_{jt}^{\beta}M_{jt}^{1-\alpha-\beta}$$ and $\alpha, \beta \in (0,1)$, \hspace{1cm} (1)

where physical gross output $Y_{jt}$ in firm $j$ at time $t$ is produced using technology indexed by $A_{jt}$ and combining labor input $N_{jt}$, capital input $K_{jt}$, and intermediate production factors (including energy) $M_{jt}$. Importantly, our data allow us to account for idiosyncratic price differences across firms, so that our measure of technology (the Solow residual, $A_{jt}$) refers to physical total factor productivity (TFPQ), rather than to revenue total factor productivity (TFPR) in the terminology of Foster et al. (2008). Equation (1) presupposes a constant-returns technology, which is an assumption we maintain in our main specification, but we also present robustness exercises where we relax this assumption. Note, however, that only the long-run returns are relevant for our empirical implementation, making decreasing returns to scale a less likely scenario.

For simplicity, and in line with the previous literature, we (for now) represent the firm-level demand curve by a constant-elastic function according to

$$Y_{jt} = \left(\frac{P_{jt}}{P_t}\right)^{-\sigma}Y_t\Omega_{jt}$$ and $\sigma > 1$, \hspace{1cm} (2)

where $P_{jt}/P_t$ is the firm’s relative price, $Y_t$ denotes aggregate market demand, and $\Omega_{jt}$ is a firm-specific demand shifter. The parameter $\sigma$ denotes the elasticity of substitution between different competing goods and hence captures the demand elasticity for each firm in the economy. Here, we let $\sigma$ represent a constant demand elasticity, but below we show that our identification remains consistent if we treat $\sigma$ as a function of the shocks, i.e. $\sigma = \sigma(A_{jt}, \Omega_{jt})$, allowing for Kimball (1995)-style strategic complementarity in price setting.

Following Guiso et al. (2008) and Franco and Philippon (2007) we model the key shocks as permanent shifters. More precisely, we specify the evolution of the demand
and technology shifters as in Franco and Philippon (2007):

\[
A_{jt} = A_{jt-1} e^{\mu^a_j + \Phi^a(L) \eta^a_{jt}}, \quad (3)
\]

\[
\Omega_{jt} = \Omega_{jt-1} e^{\Phi^w(L) \eta^w_{jt}}, \quad (4)
\]

where \(\mu^a_j\) and \(\mu^w_j\) are constant drifts, and \(\Phi^a(L)\) and \(\Phi^w(L)\) are polynomials in the lag operator, \(L\). The white-noise idiosyncratic technology and demand shocks are denoted by \(\eta^a_{jt}\) and \(\eta^w_{jt}\). The assumed functional form implies that the shocks' lag polynomials are linearly related to the log differences of \(A_{jt}\) and \(\Omega_{jt}\), respectively.\(^{12}\) As is evident from the formulation, our focus is on permanent shocks, but in a variation of the model we also explicitly analyze the role of transitory disturbances (see section 5.2).

Our model also allows for sectoral shocks to factor prices other than labor. This is potentially important in the Swedish setting of a small open economy where factor prices are likely to vary across sectors and time (due to exchange-rate volatility, for example).\(^{13}\) To simplify the notation, we next define a price index (consistent with cost minimization) for input factors other than labor, \(P^F_{jt}\) evolves according to

\[
P^F_{jt} = P^F_{jt-1} e^{\mu^f_j + \Phi^f(L) \eta^f_{jt}},
\]

where \(\mu^f_j\) is a firm-specific drift, \(\Phi^f(L)\) is a polynomial in the lag operator, \(L\), and \(\eta^f_{jt}\) is a white-noise factor-price shock.

The specified shocks (together with aggregate conditions) are taken as state variables during firm-level wage determination. In addition, we assume cost minimization and that the firms have the right-to-manage so that factor choices are made taking wages as given.

### 2.2 Identifying Long-Run Restrictions

We rely on the stylized model presented above to derive a set of long-run restrictions that allow us to filter out the structural shocks of interest (\(\eta^a\) and \(\eta^w\)). Table 1 summarizes the set of equations that motivate our restrictions, and Appendix A presents details and derivations. The second column of the table denotes variables that can all

\(^{12}\) This, in turn, provides a convenient moving average (MA) representation of the VAR specified below (see Appendix C for details).

\(^{13}\) Allowing for a factor price shock and, as discussed below, including a residual variable to soak up remaining transitory variation helps our VAR to pass standard diagnostic tests.
be constructed from our firm-level data as long as we have an estimate of the demand elasticity $\sigma$ (as detailed in the next section).

The third column summarizes the three key predictions that we rely on for identification:

1. The measured physical Solow residual ($TFPQ$ in the terminology of Foster et al. 2008) is equal to $A$ and hence independent of both demand ($\Omega$) and factor prices ($P^F$).

2. The “wage-neutral” unit labor costs ($WNULC$), as defined in the second row, is a function of both $A$ and $P^F$.

3. The “wage-neutral” demand ($WND$), as defined in the third row, is a function of $A$, $\Omega$, and $P^F$.

We use the modifier “wage-neutral” to highlight that the measures are defined to neutralize the impact of potential wage shocks. The variables are constructed in order to deliver a set of recursive long-run restrictions that we can use for identification.

Table 1: The Core Structural VAR Equations

<table>
<thead>
<tr>
<th>Column</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Variable: Measured in data as:</td>
<td>Model expression:</td>
<td>Long-run restrictions:</td>
<td></td>
</tr>
</tbody>
</table>
| $Solow$ | $Y_{jt}$ $\left(N_{jt}^\alpha K_{jt}^\beta M_{jt}^{1-\alpha-\beta}\right)^{-1}$ | $A_{jt}$ | Independent of $\eta^\omega$ and $\eta^f$
| $WNULC$ | $\left(W_{jt}N_{jt}/Y_{jt}\right)W_{jt}^{-\alpha}$ | $\alpha^{1-\alpha}A_{jt}^{-1}P_{jt}^F$, | Independent of $\eta^\omega$
| $WND$ | $Y_{jt}W_{jt}^{\sigma\alpha}$ | $\psi Y_t P_t^\sigma A_{jt}^\sigma (P_{jt}^F)^{-\sigma} \Omega_{jt}$ | $-$

Note: $Solow$ is the physical Solow residual ($TFPQ$), $WNULC$ is wage-neutral unit labor cost and $WND$ is wage-neutral demand. $\psi$ is a constant such that $\psi \equiv \left(\frac{1}{\alpha}\right)^{-\sigma\alpha} \left(\frac{\sigma}{\sigma-1}\right)^{-\sigma}$.

The recursive sequence of restrictions are highlighted in the fourth column: The Solow residual is independent of the innovations $\eta^\omega$ and $\eta^f$, and $WNULC$ is independent of $\eta^\omega$. If invoked in the long run, these restrictions are sufficient to identify a VAR model in these variables using standard structural VAR (SVAR) techniques. In practice, we will also include a fourth residual variable in the system and allow for a fourth shock that will soak up all remaining transitory dynamics in the system. We impose that this fourth shock has no long-run impact on the three variables within our
core system. Results are not sensitive to the particular choice of this fourth variable, as shown by specifications using employment, output or sales per worker. We return to this issue below.

At this stage, we would like to emphasize four features related to the key benefits of our empirical approach:

First, it is important to note that we only need to impose the zero-impact restrictions of the last column in the long run. Hence, we do not make any assumptions regarding the short-run dynamics or about transitory measurement errors. Notably, our identification of the technology shocks ($\eta^a$) are therefore consistent with changes in inventories, factor utilization, markups, or idiosyncratic input prices altering the Solow residual as long as these changes are mean reverting, i.e., as long as they do not affect the Solow residual in the long run.

Second, we do not require that all aspects of the model are true, even in the long run. We only require that the impact of the shocks on the three variables (Solow, $WNULC$, $WND$) measured in column (1) of Table 1 does not violate the restrictions listed in column (3) of the same table. These restrictions are in fact consistent with a wider class of models than the one we used to derive the restrictions.\footnote{The essential assumptions are non-restrictive relative to a broad class of possible models. The key assumptions are cost minimization, the relevance of the first order approximation of the production function, the assumption of monopolistic competition and an assumption that firms has the "right to manage", i.e. that firms make employment decisions taking wages as given (regardless of whether they are set in bargaining or not).} A particular possible extension, that for reasons presented below will turn out to be useful, is inspired by the literature on strategic complementarity in price setting (Kimball, 1995). To allow for such effects, we can let the elasticity of demand (and thereby the markup) be affected by technology and demand shocks. This replaces equation (2) by

$$Y_{jt} = \left( \frac{P_{jt}}{P_t} \right)^{-\sigma(A_{jt},\Omega_{jt})} Y_t \Omega_{jt}, \quad \sigma(A_{jt},\Omega_{jt}) > 1 \text{ and } \sigma(\bar{A}_{jt},\bar{\Omega}_{jt}) = \sigma, \tag{5}$$

where a bar denotes an average across firms. Importantly, the only change relative to the measurement equations outlined in Table 1 is that the measure of wage-neutral demand ($WND$) acknowledges that $\sigma$ is no longer constant, i.e. $Y_{jt} W_{jt}^{\sigma(A_{jt},\Omega_{jt})}$. The modified model-expression (for column 2, in Table 1) of $WND$ is thus $WND = \psi(A_{jt},\Omega_{jt}) Y_{it} P_t^{\sigma(A_{jt},\Omega_{jt})} A_j^{\sigma(A_{jt},\Omega_{jt})} (P_{jt}^F)^{-\sigma(A_{jt},\Omega_{jt})} \Omega_{jt}$ and the long-run zero restrictions of column 3 of Table 1 remain unchanged.
Third, as we show in Section 4, the approach is completely robust to potential missmeasurement of $\sigma$ since this parameter only enters on the third row of Table 1 with (as we show) a very low weight.

Fourth, the key assumption for distinguishing technology shocks from demand shocks is that technology shocks alter the physical Solow residual in the long run, whereas other shocks do not. This assumption implies that changes in the scale of operation are not allowed to permanently alter the efficiency of production as measured by TFP. The most straightforward reason why this assumption may prove invalid is that firms might use a production technology with non-constant returns to scale. It is, however, straightforward to incorporate non-constant returns to scale into the model.\footnote{Details regarding the necessary modifications for non-constant returns to scale cases, are found in Appendix A} In Section 4, we provide versions of the model where we vary the returns to scale across the full reasonable range.

### 3 Data and Estimation of the Shocks

#### 3.1 Data and Measurement

Our primary data source is the Swedish Industry Statistics Survey (IS). It contains annual information on inputs, outputs, and firm-specific producer prices for all Swedish manufacturing plants with 10 employees or more from 1990 through 2002. We perform our analysis at the plant level, but because about 72 percent of the observations in our sample pertain to plants that are also firms, we refer to the plants as firms.

In our model, the technology shock $\eta^a$ is the only shock that affects the Solow residual in the long run. This assumption is only credible if the Solow residual is calculated from a measure of real output where nominal output has been deflated by firm-specific prices. This is important because gross output deflated by sector-level price deflators (a measure often used in empirical analyses) will be a function of firm-specific idiosyncratic prices, which themselves are likely to depend on shocks other than technology (see Carlsson and Nordström Skans, 2012, for direct evidence). As our data-set contains a firm-specific price index built from plant-specific unit price changes,\footnote{The index uses Paasche-type links. In cases where a plant-specific unit-value price is missing (e.g., when the firm introduces a new good), Statistics Sweden uses a price index for similar goods defined} we can derive a measure of gross output that is robust to changes in relative...
prices across firms. See Eslava et al. (2004) and Smeets and Warzynski (2013) for a similar strategy.

To take our model to the data, we rely on gross output throughout. We first compute a measure of firm-level changes in the physical Solow residual for firm \( j \) at time \( t \). Letting lowercase letters denote logs, we use

\[
\Delta a_{jt} = \Delta y_{jt} - \Delta z_{jt},
\]

where \( \Delta y_{jt} \) is the growth rate of real gross output, and \( \Delta z_{jt} \) is a cost-share-weighted input index defined as \( C_K \Delta k_{jt} + C_N \Delta n_{jt} + C_M \Delta m_{jt} \) where \( \Delta k_{jt} \) is the growth rate of the capital stock (see details in Appendix B), \( \Delta n_{jt} \) is the growth rate of labor input, and \( \Delta m_{jt} \) is the growth rate of intermediate materials and energy. \( C_J \) terms are the cost shares of factor \( J \) in total costs. To calculate the cost shares, we use industry-level averages over time and take total costs as approximately equal to total revenues. The cost share of capital is then given by one minus the sum of the cost shares for all other factors.\(^{17}\)

Using data on factor compensations, changes in output, and changes in inputs, we can thus calculate the residual \( \Delta a_{jt} \), which provides an estimate of changes in the physical Solow residual. As argued above, this might not accurately measure technology shocks \( (\eta^a) \) due to varying factor utilization, inventories, or truly idiosyncratic factor prices, but the SVAR will filter out true technology shocks from equation (6) as long as \( \eta^a \) is the only factor that permanently shifts \( A_{jt} \). Material inputs are deflated using three-digit sectoral price indices, which implies that we allow, not only for an arbitrary set of transitory factor price shocks, but also for permanent input price shocks within the manufacturing sector as long as these are shared with other similar (at the 3-digit level) firms.

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\(^{17}\)Our monopolistic-competition model outlined above implies pure economic profits. However, similar to U.S. evidence discussed in e.g. Basu, Fernald, and Shapiro (2001), we find a very small time average (1968 – 1993) for the share of economic profits ( -0.001 ) when relying on the aggregate Swedish manufacturing data from Carlsson (2003) and a no-arbitrage condition from neoclassical investment theory (taking the tax system into account) to calculate the user cost of capital. This finding thus support the commonly used approximation in the literature of measuring (average) cost shares by (average) revenue shares, which is also used here. For simplicity, however, we do not complicate the cost structure in our model in order to explicitly accommodate the absence of economic profits in the data.

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at the minimal level of aggregation (starting at the four-digit goods-code level). The disaggregated sectoral producer-price indices are only used when a plausible goods-price index is not available. Our identification is fully resilient to transitory errors in measured prices.

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12
We next compute $\Delta wnulc_{jt}$ and $\Delta wnd_{jt}$. Relying on cost minimization, we use $C_N$ as the estimate of $\alpha$ and thus let it vary by two-digit industry. The rest of the components of $\Delta wnulc_{jt}$ are directly observed in the firm-level data. However, to compute wage-neutral demand ($\Delta wnd_{jt}$) we also need an estimate of the demand elasticity $\sigma$. We obtain this by estimating the demand equation (2) while instrumenting the firm idiosyncratic price using the Solow residual, as in Foster et al. (2008). The instrument is consistent with our initial assumptions, because the Solow residual is expected to affect firm-level sales only through firm-level prices. The results of this procedure suggest an elasticity of substitution equal to 3.306 (s.e. 0.075), which we use when computing $\Deltawnd_{jt}$. The $\sigma$ estimate is well in line with standard calibration exercises (see e.g., Erceg, Henderson, and Levin, 2000) as well as recent Swedish micro-evidence provided by Heyman, Svaleryd, and Vlachos (2008). As robustness checks, we also show that the main results are robust to using sector-specific estimates of $\sigma$ and to using a very wide span of assumed values of $\sigma$.

We extract our baseline shocks by estimating a VAR on a sample of 6,137 firms and 53,379 firm/year observations (see Appendix B for additional details on the data and for details on the construction of the final sample). Since the VAR model uses lags, we can extract structural shocks for 41,105 firm/years.

To analyze the impact of the shocks on the use of labor and the flows into and out of the firms, we link a longitudinal employer-employee data base (Statistics Sweden’s register-based labor market statistics, or RAMS) to the firm-level data. These data are based on tax records and include the identity of all employees within the plants at the end of the year (November). We restrict the analysis to full-time employees within their main jobs. In the end, we are able to match shocks and labor flows for 40,451 firm/year observations in 6,125 firms. The final sample covers nearly two-thirds of all manufacturing employees.\footnote{Note that the employment data used to construct the variables in the VAR are obtained from a different source (IS) than the employment, hiring and separation data used in the final analysis (which is obtained from RAMS). This insulates the analysis from the threat of joint measurement errors in the calculation of the shocks and the employment adjustment analysis. Estimates of the impact of the shocks on overall employment are, however, very similar using the two data sources, suggesting that the issue is of minor importance.}
3.2 Estimation

To derive the shocks of interest, we estimate a SVAR on the three variables defined in Table 1: $\Delta a_{jt}$, $\Delta wnulc_{jt}$, $\Delta wnd_{jt}$, which are constructed in order to provide us with the recursive set of long-run restrictions we need to identify the structural shocks, and a fourth residual variable (which will be output, $\Delta y_{jt}$, unless otherwise noted) which will soak up any remaining residual transitory dynamics. In practice, we first estimate four reduced-form equations where $\Delta a_{jt}$, $\Delta wnulc_{jt}$, $\Delta wnd_{jt}$, and the residual variable are explained by two lags of all four variables. We then invoke the long-run restrictions (including the long-run independence of the core system to the fourth residual shock) to derive the impulse responses of the structural shocks. Details regarding identification and estimation are found in Appendix C.

The specification includes firm-specific fixed effects to capture the drift terms of equations (3) and (4) as well as year dummies to capture aggregate shocks shared by different firms within the manufacturing sector, hence allowing us to concentrate on idiosyncratic disturbances. As a robustness check, we also use specifications accounting for sector-specific year dummies.

We use dynamic panel data methods building on Arellano and Bond (1991) for estimation because the asymptotic properties of the estimator rely on the cross-sectional dimension. This is a very useful feature in the current context of a large $N$ (6,137 firms), but short $T$ (12 years) panel because the identification of structural shocks with long-run restrictions crucially hinges on the quality of the estimated reduced-form coefficients and covariance matrix.

Table 2 shows descriptive statistics of the structural shocks derived for our baseline sample and specification. The standard deviation of the demand shock is about 60 percent larger than the technology shock (16.2 and 10.1, respectively). Appendix C depicts the shock distributions in graphs and also shows impulse responses and variance decompositions related to the main SVAR model. In addition, the appendix discusses specification tests.

Two particular results are relevant for the analysis ahead. First, we find a fairly limited amount of dynamics, in particular in the Solow residual. The main reason for this finding is that the Solow residual is defined in physical gross terms and much of the dynamics in standard measures of Solow residuals appear to be due to the dynamics of idiosyncratic prices (see Carlsson and Nordström-Skans 2012, for direct evidence on relative-price dynamics). Second, shocks to the residual fourth variable
explain little of the variance in our key variables at all horizons. Since the VAR model is estimated conditional on time dummies, this finding is in line with the result of Franco and Philippon (2007), which shows that transitory shocks, although highly correlated across firms (and therefore of macroeconomic importance), matter only marginally at the firm level.

Table 2: Demand and Technology Shocks

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
<th>(6)</th>
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<tbody>
<tr>
<td></td>
<td>Mean</td>
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<td>p(25)</td>
<td>p(75)</td>
<td>Firms</td>
<td>Observations</td>
</tr>
<tr>
<td>Technology ($\eta^t$)</td>
<td>– 0.101</td>
<td>-0.056</td>
<td>0.058</td>
<td>6,137</td>
<td>41,105</td>
<td></td>
</tr>
<tr>
<td>Demand ($\eta^d$)</td>
<td>– 0.162</td>
<td>-0.086</td>
<td>0.085</td>
<td>6,137</td>
<td>41,105</td>
<td></td>
</tr>
</tbody>
</table>

Note: p(N) denotes the Nth percentile of the data.

### 3.3 Validation

Because the shocks we are analyzing are idiosyncratic, we cannot use correlations with known aggregate shocks such as oil-price or exchange-rate movements to cross-validate their interpretation, at least not without strong priors regarding differences between firms in the sensitivity to these aggregate shocks. Instead, we perform two alternative corroboration exercises.

A first piece of evidence supporting our interpretation of the shocks is presented in Appendix C, which shows theory-consistent signed impulse responses for the three unrestricted responses within the VAR system: The estimated response of $\Delta w_nulc_{jt}$ to a technology shock is negative, as predicted from the theoretical model. Similarly, the estimated responses from both technology shocks and factor prices on $\Delta wnd_{jt}$ are negative.

A second piece of evidence comes from relating the permanent shocks to the firm-specific price index and to output. If technology shocks only affect the cost of production, we should expect technology shocks to reduce prices since firms would need to set lower prices in order to increase their sales along a fixed demand curve. In contrast, demand shocks, defined as shifts in the firm-specific demand curve, allow the firm to sell more at a given price. This suggests that prices should remain unchanged or increase under reasonably pricing strategies.

Hence, economic theory suggests that both technology and demand shocks should affect output, whereas prices should fall if the output increase is due to a technology
shock (but not if it is due to a demand shock). To assess these general predictions, we reestimate the SVAR and compare responses of output and prices to the two shocks (using output and prices, in turn, as the fourth variable in the SVAR system).

Figure 1 shows the impulse responses of output and idiosyncratic prices to technology and demand shocks—indicating that both types of shocks are important for firm-level aggregates. The figure also clearly validates the general predictions discussed above: A 1 standard deviation (sd.) technology shock increases output by 6 percent in the long run. In the case of a 1 sd. demand shock, output rises by 10 percent. Moreover, as expected, prices go down in the case of a technology shock. In contrast, prices increase slightly when the demand curve shifts. In our view, the finding that the demand shock permanently changes output without lowering relative prices strongly supports the interpretation of the demand shock as an idiosyncratic shift in the demand curve. Note that these results are not imposed from the construction of our variables: in particular, prices could well (from a pure measurement standpoint) respond in either direction to structural innovations in both technology and demand.

4 Results

4.1 Idiosyncratic Shocks and Employment Adjustment

A first objective of our analysis is to illustrate how firm-level employment responds to permanent shifts in idiosyncratic production functions and demand curves. Figure 2 shows impulse responses of log employment with bootstrapped confidence bands. The responses are derived from our SVAR system, using employment as the fourth variable.

The figure shows that idiosyncratic demand shocks have substantially more impact than the corresponding technology shocks on firm-level labor adjustments. A positive demand shock of 1 sd. increases employment by slightly more than 6 percentage points, whereas the impact of an equivalent technology shock raises employment by only 0.5 percentage points. It is also evident from Figure 2 that the dynamics of labor adjustments are fairly limited. More than 90 percent of the long-run adjustments in response to the permanent shocks occur within the first year. We return to a discussion regarding the magnitudes in Section 4.1.2 below.
Much of the analysis that follows below relies on exploring non-linear responses to the estimated shocks. In order to estimate these responses, we proceed in three steps: We (i) estimate the SVAR, (ii) extract the ensuing measures of structural shocks, and (iii) relate the shocks to different outcomes in a standard regression framework. This gives us additional flexibility in the specifications, which will be exploited in the next sections to assess potential asymmetries and non-linearities in the labor adjustment responses and allows us to present the results in a more compact table format. Empirically, we estimate the following equation in the (linear version of the) baseline specification:

\[
\text{Outcome}_{jt} = \eta_{jt}^{o} \delta_{1} + \eta_{jt}^{d} \delta_{2} + \rho_{t} \beta_{p} + \mu_{j} + \xi_{jt},
\]  

(7)

where \textit{Outcome} denotes employment (or hires and separations in the following sections) for firm \(j\) at time \(t\). The coefficients \(\delta_{1}\) and \(\delta_{2}\) capture the impact of the firm-level
Figure 2: Employment Responses

Note: Impulse responses to a 1 sd. shock expressed in percentage points. Lines depict the mean of the bootstrap distributions. Shaded areas depict the bootstrapped 95 percent confidence intervals calculated from 1,000 replications.

structural shocks on the outcomes.\textsuperscript{19} Moreover, we include time, $\rho_t$, and firm-fixed effects, $\mu_j$, in line with the SVAR formulation above. This ensures that identification is driven by idiosyncratic, rather than aggregate, shocks.\textsuperscript{20} Equation (7) shows the short-run impact of the shocks. We also present the long-run impact, measured as the sum of the contemporary effect and the impact of the first lag in the shock series.

Our baseline specification, following equation (7) is presented in the first column of Table 3, and as is evident (and expected), the results closely mimic the impulse responses presented in Figure 2: In the short run, employment increases by 6 percentage points in response to a positive demand shock of 1 sd. The coefficient of an equivalent technology shock is 0.15, and is not statistically different from 0. If we add one lag of the shocks to the regression and calculate the long-run employment responses (column 4), the technology shock becomes somewhat larger and also statistically significant. However, long- and short-run responses are of a fairly similar magnitude, which corroborates our findings of limited dynamics in the labor adjust-

\textsuperscript{19} Formally, the inference is exposed to a potential generated regressor bias, but we show that all key results hold when either estimating them internally in the VAR or when relying on an IV-strategy (see below), both of which are insensitive to generated regressor biases.

\textsuperscript{20} Since the shocks are identified as structural orthogonal innovations, they are uncorrelated with each other conditional on the year and firm-fixed effects of the SVAR.
ment. As before, firms’ demand shocks continue to be the main driver of employment adjustments: A positive 1 sd. shock to the demand curve increases employment in the long run in 6.4 percentage points, while the equivalent technology shock increases employment by 0.5 percentage points.

Table 3: Contemporaneous and Long-Run Effect on Log Employment under Different Returns to Scale Assumptions

<table>
<thead>
<tr>
<th>SHORT RUN</th>
<th>LONG RUN</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) RTS=1</td>
<td>(2) RTS=0.9</td>
</tr>
<tr>
<td>Technology ($\eta^T$)</td>
<td>0.153</td>
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<tr>
<td>Demand ($\eta^D$)</td>
<td>5.986**</td>
</tr>
<tr>
<td>Observations</td>
<td>40,451</td>
</tr>
<tr>
<td>Firms</td>
<td>6,125</td>
</tr>
<tr>
<td>Sd. $\eta^T$</td>
<td>10.06</td>
</tr>
<tr>
<td>Sd. $\eta^D$</td>
<td>16.18</td>
</tr>
</tbody>
</table>

Note: Effect of one s.d. shock. Robust standard errors in parenthesis. Regression includes firm fixed effects and time dummies. Long-run estimates are obtained by adding the contemporaneous impact and one lag. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.

The constant returns to scale (RTS) assumption used in the construction of the Solow residual is potentially controversial. In Carlsson, Messina, and Nordström-Skans (2014), we estimate RTS separately for the durables and non-durables sectors among Swedish manufacturing firms, obtaining 1 for durables and 0.9 for non-durables. In both cases we cannot reject the null of constant RTS. These results are very similar to what Basu, Fernald, and Kimball (2006) report for the U.S. Note also that what matters is the long-run returns to scale which implies that the theoretical case for assuming constant returns to scale becomes stronger.

The model can be altered to accommodate increasing or decreasing RTS. Changing the assumed RTS affects the measures that are fed into the SVAR (for details, see Appendix A) and hence also the estimated magnitudes of employment adjustments. However, the main message remains robust throughout. Column 2 in Table 3 reports results from imposing RTS of 0.9 in the construction of the Solow residual. A positive technology shock of 1 sd. raises employment now by 1 percentage point in the short run (1.4 in the long run, see column 5). But this estimate still remains far below the
estimated impact of a demand shock: an increase of 6.1 percentage points in the short run and 6.3 in the long run. If instead we impose an RTS coefficient of 1.1, the results change in the other direction (the impact of technology turns negative), but the main message regarding the strong relative importance of demand remains unaltered.

4.1.1 Robustness

We proceed by carrying out a battery of checks to assess the robustness of our first set of findings—namely, that (i) firm-level demand shocks are more important in the determination of labor adjustments than firm-level technology shocks, and (ii) employment adjustment to the permanent shocks is very rapid, exhibiting limited short-term dynamics. In all cases we use the specification presented in equation (7). We discuss the main findings here, but present the regression tables in Appendix D to conserve space.

Demand elasticity. The baseline specification uses an estimated demand elasticity of 3.3. As a robustness check we have verified that our key results are robust to demand elasticities that vary within what we believe to be the full range of plausible values (from 1.1 to 10); the results in Table D1 (columns 2 and 3) show that the estimated coefficients of technology and demand shocks are remarkably stable despite this large interval of measured demand elasticities. Additional tests in Table D1 allow for industry-specific estimates of the demand elasticity, and as shown in column 4 of the table, this does not alter the results. The reason for this robustness is that measured $\sigma$ only enters our system in order to handle idiosyncratic wage movements, and these are much smaller than the movements in output which it is weighted against.\(^{21}\) The main results also stay unaffected if we instead replace the year dummies by industry-by-year dummies, which controls for different employment trends across sectors (column 5).

Sectoral heterogeneity. The dynamic panel approach used for estimation took advantage of our large-$N$ small-$T$ panel setting to estimate the VAR system with considerable precision. This is a key advantage relative to standard SVAR estimations in the macro literature. A potential cost, however, is that the underlying dynamic

\(^{21}\)To recap, $\Delta w_{n,t} = \Delta y_{t} + \sigma(\alpha* \Delta w_{jt})$. In the data, the within-firm standard deviation in $\Delta y_{jt}$ (0.326) is seven times larger than the within-firm standard deviation in $\alpha \Delta w_{jt}$ (0.046). Furthermore, the two elements are positively correlated (0.27). As a consequence, the within-firm correlation between $\Delta w_{n,t}$ as measured with $\sigma = 1.1$, and $\Delta w_{n,t}$ as measured with $\sigma = 10$, respectively, is 0.81.
processes are assumed to be equal across different firm types. To address this concern, we have allowed for separate dynamics for each two-digit industry, and the employment adjustment results remain unchanged (see column 6 in appendix Table D1).

Sample selection. The data appendix (Appendix B) explains that the output allocation across plants within (the relatively few) multi-plant firms after 1996 is imputed in the IS data set. We have therefore redone the analysis for the single-plant firms in the sample (column 2 of appendix Table D2), as well as for a mixed sample including multi-plant firms until 1996, but not thereafter (column 3 of Table D2). The results are robust in these alternative samples which is not surprising since the bulk of the original sample is unaffected. The results are also unchanged when the shock distribution is truncated into the Lester range of \(-2\) to 2 sd. (see column 4 of Table D2).

Alternative fourth variable in the SVAR. To ensure that the limited dynamics in the employment adjustments we find is not due to the specific way we handle the residual dynamics in the system, we have used sales per worker, output, and employment from our two data sources (RAMS and IS) as alternative fourth variables. Table D3 shows that these variations only have minor impacts on both the estimated dynamics and the long-run adjustments.

Firm exit. Finally, a possible concern with the analysis is that we disregard the firm-exit process. Firms are likely to exit in response to severe negative demand or technology shocks, and this process may impact labor dynamics. To address this concern, we have analyzed the employment impact of the shocks using a two-periods specification instead of the one-period baseline (see Appendix Table D4). In practice, this implies that we relate the shock to the net employment growth across two years, defined as the change in employment divided by the average employment in the two years as in Davis et al. (1996). Since the labor flows are defined even if all workers exit the year after the shock, we can calculate the impact of the shocks while excluding or including the firms that exit. Reassuringly, the results are insensitive to whether we include or exclude exiting firms.

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22 As explained in Section 3, 72 percent of plants are in single-plant firms and the imputation only affect the later half of the sample.
23 That the fourth variable plays a negligible role in employment adjustment is also suggested in the variance decomposition shown in Appendix C.
24 We have also analyzed the explicit relationship between the shocks and the probability of firm exit from the sample. The main driver of firm exits are large negative demand shocks which is well in line with results for the United States in Foster, Haltiwanger, and Syverson (2008).
Overall, our findings strongly suggest that (i) permanent shifts in firms’ idiosyncratic demand curves are a key determinant of firms’ idiosyncratic net employment adjustments, and (ii) the pace of labor adjustment is relatively fast. In contrast, permanent shifts in firms’ physical production functions (i.e., technology shocks) appear to play a much more limited role in firms’ labor adjustment, despite being crucial to the evolution of both output and relative prices.

4.1.2 Discussion of Magnitudes

The impact of technology shocks on employment is small, but fully in line with the finding of Pozzi and Schivardi (2015) for the Italian manufacturing industry. In particular, if assuming constant (decreasing) returns to scale our implied elasticity of the technology shock is 0.05 (0.14), whereas Pozzi and Schivardi (2015) find 0.08.\(^\text{25}\)

The key novel finding relative to the previous studies is instead the strong employment effect we find from the demand shocks.\(^\text{26}\) Here, it is worth noting that our demand shocks are permanent, and these are likely to have a much larger impact than transitory shocks. We return to this issue in Section 5.2.

It is, however, also notable that the relative responses of some of the key variables are difficult to reconcile with the constant-\(\sigma\) model which has been used in most of the literature so far, including Foster, Haltiwanger, and Syverson (2008), Foster, Haltiwanger, and Syverson (2012) and Pozzi and Schivardi (2015) (when operating below full capital utilization), and which we also used to derive the restrictions in Section 2. The model predicts that employment responses to technology and demand shocks are related by a factor of \(\frac{1}{\sigma-1}\) (in our case; only in the long-run). The empirical employment responses would thus suggest that \(\sigma\) should be smaller than the value of 3.3 which we use in the measurement of \(WND\). Although we could, as shown above, in principle choose any reasonable number for \(\sigma\) without affecting the results, the single parameter \(\sigma\) pins down all responses of prices, output and employment according to the standard constant-\(\sigma\) model (see Appendix A.2 for the full Jacobian).

\(^{25}\)Pozzi and Schivardi (2015) find strongly decreasing returns to scale (0.8) for Italian firms in the textile, leather, metals and machinery sectors. This is lower than the average overall manufacturing returns to scale that has been found for Sweden, see e.g. Carlsson, Messina, and Nordström-Skans (2014) and the U.S., see e.g. Basu, Fernald, and Kimball (2006). The qualitative conclusions hold even if we impose a returns to scale of 0.8 however (demand is still three times as important as technology).

\(^{26}\)The implied employment elasticity is 0.39, compared to, e.g., 0.08 found by Pozzi and Schivardi (2015)
Unsurprisingly, we are unable to simultaneously match all of these responses regardless of which value we choose for \( \sigma \).

However, due to the flexible nature of our identifying restrictions, it is possible to write down extended versions of the theoretical model which can be reconciled with our identifying assumptions and which would allow us to match the empirical results much better. Given the fact that our observed price response to the technology shock is substantially smaller than the unit response implied by the standard constant-\( \sigma \) model, the data seem to ask for a model that is richer in its description of product market responses to the shocks. A straightforward generalization in this direction is to assume that the elasticity of demand (and thereby the markup) can be affected by technology and demand shocks, i.e. a model where we replace \( \sigma \) by the function \( \sigma(A_{jt}, \Omega_{jt}) \) as already hinted at in Section 2. The extension is discussed in more detail in Appendix A.2. Despite the fact that the long-run restrictions remain identical if we modify the model in this dimension, the modification dramatically changes the structural interpretation of the results. As described in Appendix A.2, optimally choosing derivatives of \( \sigma(A_{jt}, \Omega_{jt}) \) allows us to match the empirical responses to the augmented model well. Notably, the derivatives suggest a very moderate (-0.6) reduction in \( \sigma \) from a 1 standard deviation technology shock and an even smaller reduction in the case of a demand shock (-0.1). Obviously, both are tiny compared to the variations of \( \sigma \) (from 1.1 to 10) considered in our robustness exercises discussed above.\(^{27}\) The key takeaway from this exercise is, however, that the empirical results are consistent with our identifying long-run restrictions, and with a theoretical model that allows for more flexible relative price responses to the shocks.

### 4.2 Idiosyncratic Shocks, Hires, and Separations

To analyze which margins firms use to adjust employment when hit by permanent idiosyncratic demand and technology shocks, we relate our measures of shocks to firm-level measures of worker flows (i.e., hires and separations). Using annual individual-level employment data on end-of-the-year employment that are matched to our firm-level data, we compute measures of job and worker flows using the metrics proposed

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\(^{27}\)Interestingly, the results imply that the firm increases the markup slightly in response to a one standard deviation technology shock (0.11) whereas the markup is nearly unaffected by the demand shocks (0.02) which is in line with the standard “smoothed-off kinked” demand-curve interpretation suggested by Kimball (1995).
by Davis et al. (1996).

Net employment growth is defined as the change in employment relative to the preceding year, divided by the average employment during the two years. Similarly, we define the hiring (separation) rate as the number of new (separated) employees between \( t \) and \( t - 1 \), divided by the average number of employees during the two years. With these definitions, net employment growth will be the difference between the hiring rate and the separation rate, and the timing of the flows are defined such that the flow equation of employment holds.\(^{28}\)

We also calculate a measure of the short-tenured (< 3 years) separation rate using the same denominator as for the other rates. All in all, we can match these flow measures to 6,130 firms in the firm data (described in Section 3). Table 4 displays descriptive statistics of these measures for the sample in which structural shocks can be constructed (40,451 observations). The average hiring rate during the observation period is 15 percent, and the average separation rate is 14 percent, whereof slightly less than half (6 percent) are separations of short-tenured workers.

We proceed analogously to the employment analysis of the preceding section. Hence, we follow equation (7) for hires and separations, separately. Table 5 present the effects of a 1 sd. technology and demand shocks in both the short and long run, as well as the corresponding elasticities (see Appendix C regarding the computation of the elasticities). A normal demand shock is estimated to increase the hiring rate by 2.9 percentage points and reduce the separation rate by 2.7 percentage points in the short run (slightly more in the long run).\(^{29}\) These numbers should be compared with average hiring and separation rates of about 14 to 15 percent each, as shown in Table 4 above. The estimates imply that, on average, 52 percent of the net employment adjustment is obtained using the hiring margin, and 48 percent using the separation margin. Firms thus, on average, rely as much on variations in separations as on variations in hires when responding to the shocks. This result is also interesting in the light of the literature on labor flows and the business cycles (see Barnichon,

\(^{28}\)That is, \( \text{Employment}_t = \text{Employment}_{t-1} + \text{Hires}_t - \text{Separations}_t \).

\(^{29}\)Note that the difference in the estimated coefficients of the hiring and separation rate result in the impact of the shocks on the net employment change (not reported in the table). However, there is a marginal difference between the implied results on employment changes presented here and those reported in columns 1 and 4 of Table 3. This arises because we here follow the metric proposed by Davis, Haltiwanger, and Schuh (1996) to measure net employment changes, instead of the log differences we relied on in the previous subsection. The differences are, however, far from altering our main conclusions.
Table 4: Summary Statistics. Worker’s data

<table>
<thead>
<tr>
<th>Category</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
<th>(6)</th>
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<tr>
<td></td>
<td>Mean</td>
<td>sd</td>
<td>p(25)</td>
<td>p(75)</td>
<td>Firms</td>
<td>Observations</td>
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<td>Net Employment Rate</td>
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<tr>
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<td>within</td>
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<tr>
<td>Hiring Rate</td>
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<tr>
<td>overall</td>
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<td>0.063</td>
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<td>40,451</td>
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<td>within</td>
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<tr>
<td>Separation Rate</td>
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<td></td>
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<tr>
<td>overall</td>
<td>0.138</td>
<td>0.152</td>
<td>0.061</td>
<td>0.174</td>
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<td>40,451</td>
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<tr>
<td>within</td>
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<tr>
<td>ST Separation Rate</td>
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<tr>
<td>overall</td>
<td>0.061</td>
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<td>0</td>
<td>0.083</td>
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<td>40,451</td>
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<td>within</td>
<td></td>
<td></td>
<td></td>
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</tr>
</tbody>
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Note: The “within” rows show the dispersion within establishments. p(N) denotes the Nth percentile of the data.

Table 5: Permanent demand and technology shocks, hirings, and separations

<table>
<thead>
<tr>
<th>SHORT RUN</th>
<th>LONG RUN</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1)</td>
<td>(2)</td>
</tr>
</tbody>
</table>

A) 1 sd. shock:

Technology ($\eta^T$)

-0.050   -0.165*   -0.117**
(0.075)  (0.078)  (0.038)

Demand ($\eta^D$)

2.906** -2.703** -1.010**
(0.096)  (0.120)  (0.052)

B) Elasticities:

Technology ($\eta^T$)

-0.005   -0.016*   -0.012**
(0.007)  (0.008)  (0.004)

Demand ($\eta^D$)

0.180** -0.167** -0.062**
(0.006)  (0.007)  (0.003)

Observations 40,451 40,451 40,451 34,414 34,414 34,414

Note: Robust standard errors in parenthesis. Hiring Rt: Hiring rate; Sep. Rt: Separation rate; ST Sep. Rt.: Short-tenured separation rate. Hiring and separation rates are measured as the flow between the end points of two years divided by the average employment across these two points in time. ST Sep. Rt. is measured as the number of separations of short-tenured (< 3 years) workers divided by the same denominator as the other rates. Regressions include time dummies and firm fixed effects. The long-run impact is based on the sum of the contemporary effect and the effect of the first lag. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.
2012; Fujita and Ramey, 2009; and Shimer, 2012). It suggests that any quantitatively important asymmetries between hiring and separations over the business cycles should be explained by asymmetries in the market responses, and not as asymmetries in firm-level labor adjustment behavior.

The results imply that the low response of net employment to technology shocks does not mask any substantive counteracting responses in terms of gross flows. Rather, idiosyncratic technology shocks appear to have a limited impact on both hiring and separation rates in both the short run and the long run. As a final result, we see that separations of short-tenured workers make up slightly more than one-third of the total short-run separation response to demand shocks, but a lower fraction of the longer-run responses.30

4.3 Asymmetry and Non-Linearity

To examine potential non-linearities in the hiring and separation responses depending on the signs and magnitudes of the shocks, we extend equation (7) by allowing for separate second-order polynomials above and below zero. Because the dynamics add few insights, we focus on the short-run impact.

Figure 3 shows how firms adjust their hiring rates in response to positive and negative shocks of different magnitudes. To facilitate the interpretation, the graphs show the sum of the average hiring rate among firms that do not adjust employment (about 10 percent) and the predicted estimates for various deviations from a zero-shock state. For completeness, we show the responses to both technology and demand shocks, but we focus our attention toward the demand-shock responses. (Throughout, we find limited adjustments in response to technology shocks, as expected from the previous subsections.)

Two patterns are particularly noteworthy: First, the hiring response is considerably smaller if the shocks are negative. Second, the impact of a 2 sd. positive shock is exactly twice that of a 1 sd. positive shock, suggesting that the costs of increasing hires are a linear function of the magnitude of the adjustment.

Figure 4 shows the corresponding patterns for separations. The shapes and magnitudes (again focusing on the demand shocks) are not far from mirror images of the

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30 The lower relative contribution of short-tenured separations in the long run is consistent with a reduction in contemporary hires, which reduces the number of short-tenured workers who can be released in the next period.
Figure 3: Shocks and the Hiring Rate

Note: Each line represents the sum of the average hiring rate among firms that do not adjust employment (10 percent) and the response of the hiring rate in percentage units as a (non-linear) function of an x sd. technology or demand shock. Shaded areas depict 95 percent confidence intervals.

impact on the hiring rate. Thus, separations primarily respond to negative shocks. Although separations do go down somewhat when shocks are positive, this impact is even smaller than the hiring cuts in response to negative demand shocks. Symmetrically to the hiring response, the estimates imply that a 2 sd. negative shock causes a separation response that is exactly twice as large as the response to a 1 sd. negative shock, which suggests that the costs of increasing separations are approximately linear on average. Notably, the results of Figures 3 and 4 imply that firms primarily use separations when responding to permanent negative demand shocks, an issue to which we return to below.

Finally, Figure 5 shows the impact on net employment and, as could be imagined from the combination of Figure 3 and Figure 4, these effects add up to a fairly linear relationship. The somewhat more curved pattern on the positive side arises because the kink at zero is more pronounced for hires than for separations. This difference in curvature is statistically significant, but the magnitude is fairly small: The net employment changes in response to a 2 sd. positive demand shock (9 percentage points) is reasonably close to the response to a 2 sd. negative shock (−13 percentage points) in absolute values.
Figure 4: Shocks and the Separation Rate

Note: Each line represents the sum of the average separation rate among firms that do not adjust employment (10 percent) and the response of the separation rate in percentage units as a (non-linear) function of an x sd. technology or demand shock. Shaded areas depict 95 percent confidence intervals.

Figure 5: Shocks and the Net Employment Rate

Note: Each line represents the response of the net employment rate in percentage units as a (non-linear) function of an x sd. technology or demand shock. Shaded areas depict 95 percent confidence intervals.
4.4 The Causal Effects of Employment Adjustments on Worker Flows

This subsection provides an analysis of how firm-level employment adjustments in response to permanent demand shocks translate into worker flows. This analysis is similar in spirit to Abowd et al. (1999), and Davis et al. (2012), which provide decomposition exercises of the relative contribution of various worker flows to the observed employment changes in French and U.S. firms, respectively. In contrast to these previous studies, however, we analyze changes in hires and separations induced by employment adjustments due to a demand shock. This allows us to obtain a causal correspondent to the decompositions in the earlier literature. In our case, demand shocks drive the changes in employment, and we can therefore abstract from, for example, possible exogenous separations which may affect firms’ employment levels in the short run.

In practice, we characterize labor adjustments by two second-order polynomials, one for positive values and one for negative values. We then instrument this adjustment by a similarly constructed set of polynomials in the demand shock. We use the hiring rate as our outcome, but since net employment adjustment is identical to the difference between hires and separations, the impact on separations is easily deduced.

The results are presented in the left-hand panel of Figure 6. They imply a strong and linear relationship between net employment adjustments and hires when the employment adjustments are positive, but a very modest relationship when the employment adjustments are negative. The right-hand panel of Figure 6 shows the share of employment adjustment through hires as a function of demand-induced net employment changes. This share jumps from 20 percent to 95 percent when employment adjustments become positive instead of negative.

Figure 6 also suggests that firms are relatively unconstrained in their use of separations, since they rely on increased separations even when they could have adjusted

\[ \text{31} \] We focus on permanent demand shocks because technology shocks are found to have negligible impacts on net employment.

\[ \text{32} \] The instrumental variable (IV) strategy essentially implies that we scale the shock impact on the hiring rate presented in Figure 3 above with the first stage, which corresponds to Figure 5.

\[ \text{33} \] Note that, in contrast to Figures 3 and 4 (where the zeros refer to the absence of an idiosyncratic shock), zero here refers to the state when net employment adjustment is predicted to be zero based on the full first stage (i.e., based on the combination of the shock polynomials, the year dummies, and the firm-fixed effects).
Figure 6: The Hiring Rate and Net Employment Changes. IV Results

Note: Left-side panel: Contemporaneous hiring rate in percentage units as a (non-linear) function of employment adjustment in percentage units. Employment adjustments are instrumented by demand shocks. Shaded areas depict 95 percent confidence intervals. Right-side panel: Implied fraction of employment adjustment achieved through changes in hirings as a function of the size and magnitude of the employment adjustment.

... through reduced hires. To make this point precise, Figure 7 repeats the patterns shown in the right-hand panel of Figure 6 but focuses on negative values. As benchmarks illustrating what the firms could have done, the figure also depicts two hypothetical adjustment curves. The first, denoted “hypothetical homogeneous,” assumes homogeneous firms and imposes the empirical steady-state (i.e., without employment changes) separation rate of 10 percent on all the firms. In this case, as long as the need for adjustment is 10 percent or less, reduced hires could fully accommodate the necessary adjustments. If the shock is 20 (30) percent instead, the firm could instead accommodate half (one-third) of the adjustment through reduced hires. Notably, this curve assumes that 10 percent of employees leave each firm every year, which clearly cannot be the case.

We therefore also provide a second benchmark, assuming instead that the individual probability of leaving a firm is 10 percent. By randomly allocating quits across the workers in our full sample and then aggregating to the firm level, we get the firm-level distribution of quit rates. With this distribution, which naturally widens if firms are small, some firms will not experience any quits at all, which means that
Figure 7: Actual (IV) and Simulated Hiring Responses to Employment Changes

Note: Actual (estimated from data) and hypothetical maximum (simulated) fraction of negative employment adjustments (in percentage units) achieved through changes in hires. Employment adjustments are instrumented by demand shocks. “Hypothetical homogenous” assumes that the same fraction of workers always leaves the firm. “Hypothetical heterogenous” imposes a random individual quit rate on the actual firm-size distribution.

they cannot accommodate even the smallest employment adjustment through reduced hires, whereas other firms will experience many random separations, allowing them to accommodate large employment reductions through reduced hires. The curve denoted “hypothetical heterogeneous” displays the simulated frontier of adjustments with random individual quits using our actual distribution of firm sizes.

The logic behind the hypothetical curves is that they provide a baseline indicating how firms would behave in a completely rigid world where firing is prohibitively costly as long as firms are hiring someone. In this case firms would always adjust according to the hypothetical heterogeneous curve in Figure 7. As is evident, the observed employment adjustments are far from this rigidity benchmark. The actual share of adjustment through reduced hires is much lower than the hypothetical reliance on separations would allow for. The shaded area between the heterogeneous hypothetical curve and the actual behavior of the firm could be interpreted as a region of flexibility because it depicts the amount of negative labor adjustments through induced separations (i.e., separations above the random rate) which could have been accomplished through reduced hires instead.
Figure 8: The Separation Rate of Short-Tenured Workers and Net Employment Changes. IV Results

Note: Left-side panel: Contemporaneous separation rate of short tenured workers in percentage units as a (non-linear) function of employment adjustment in percentage units. Employment adjustments are instrumented by demand shocks. Shaded areas depict 95 percent confidence intervals. Right-side panel: Implied fraction of employment adjustment achieved through changes in separation rate of short tenured workers as a function of the size and magnitude of the employment adjustment.

One reason for the observed patterns may be that firms adjust by releasing marginal, short-tenured workers who are more likely to be on temporary contracts. Sweden is a country with slightly above-average levels of employment protection (OECD, 2014), but the use of temporary contracts is flexible, whereas protection for workers with open-ended contracts is more restrictive. It is thus possible that the labor market responses studied here may hide important heterogeneity across workers, depending on their contract type and tenure with the firm.

We do not observe the contract type in the data, but in order to explore the role played by the (potential) flexibility provided by marginal workers, we have estimated the IV specification using the following outcome variable: separation of short-tenured (less than three years) workers divided by average employment across the two years. The results, shown in Figure 8, suggest that about half of the response to negative shocks come through reductions of short-tenured workers.

We have also repeated the simulation exercise presented in Figure 7 above, but instead contrasting the actual combined adjustment of reduced hires and increased
Note: Actual (estimated from data) and hypothetical maximum (simulated) fraction of negative employment adjustments (in percentage units) achieved through changes in hirings and short-tenured separations. Employment adjustments are instrumented by demand shocks. “Hypothetical homogenous” assumes that the same fraction of workers always leaves the firm and are employed on short tenure (less than three years). “Hypothetical heterogenous” imposes a random individual quit rate and short-tenure rate on the actual firm-size distribution.

The results, presented in Figure 9, show that firms are far from using the flexibility provided by these two margins. The substantial shaded area in the figure implies that firms rely much more on separations of long-tenured workers than they would have needed to in order to achieve the same level of net employment reduction.

5 Extensions

The results presented above suggest that labor adjustments in response to positive and negative demand shocks are fast and that separations are a flexible margin of adjustment when employment reductions are needed. This section provides two extensions that we believe shed light on the process.

We first explore, in subsection 5.1, the hypothesis that our results are driven by within-firm heterogeneity in worker skills, which may create imbalances between the
skills of those workers who quit at random and the optimal skill mix within the firm.

Thereafter, we note that if adjustments were costly, firms would be expected to hoard labor and/or refrain from hiring when shocks are perceived as temporary. The focus of the analysis so far, however, has been on how firms adjust employment, hires, and separations when hit by permanent idiosyncratic shocks. As a contrast, subsection 5.2 analyzes the role of transitory shocks to demand.

### 5.1 Firm-Level Heterogeneity

Taken at face value, our results imply that firms either bear few costs to separate long-tenured workers, or rely heavily on a well-defined mix of worker types that is hard to change when demand changes. If the latter is true, it is more than likely that the workers who leave, or who are on temporary contracts, differ from the types of workers that the firms would like to separate from. Hence, it is not possible for the firm to fully exploit worker attrition or their pool of short-tenured workers to adjust to the shock.

To explore this further, we provide estimates separately for firms with a homogenous workforce in terms of field and education level and for firms with a heterogeneous workforce in the same dimensions. The idea is that firms with a more homogenous set of employees should care less about whom they separate from and thus rely more on attrition and the separation of short-tenured workers when adjusting their net employment.

In practice, we calculate the fraction of coworkers (to each worker in the data) that has the exact same type of education (three-digit field and two-digit level) and take the average of this share for each firm. This gives an index of the average worker’s exposure to similarly trained workers within the firm (in spirit, similar to measures of workforce diversity). In a second step, we split our firm-level data across the median of this index and analyze the two samples separately.

Figure 10 presents the results for the two samples, i.e., for firms with high versus low degrees of educational similarity among workers. As before, we characterize labor adjustments by two second-order polynomials, one for positive values and one for negative values. We then instrument this adjustment by a similarly constructed set of polynomials in the demand shock.

Quite surprisingly, we find little support for the notion that within-firm heterogeneity is an important explanation for the low reliance on separations when firms
Figure 10: The Hiring Rate and Net Employment Changes: Firm Size and Worker Heterogeneity. IV Results

Note: Contemporaneous hiring rates in percentage units as a (non-linear) function of employment adjustments (in percentage units) in subsamples defined by employee heterogeneity (lower graphs) and firm size (higher graphs). Employment adjustments are instrumented by demand shocks. Low (high) similarity firms are those with a similarity index (described in the text) below (above) the median. Small (large) firms are those with fewer (more) than 20 employees. Shaded areas depicts 95 percent confidence intervals.

are hit by negative demand shocks. We would, however, like to acknowledge that our measures of staff heterogeneity may well be too crude to capture the role of firm-level heterogeneity in the adjustment patterns.

Figure 10 also shows results separately by firm size (more than 20 employees or fewer than 20 employees). The idea is again that if worker heterogeneity is important for the results, smaller firms are more likely to have difficulties using attrition and separation of short-tenured workers to adjust their staffs. The results, however, are very similar across the two size classes, displaying as before little signs of systematic heterogeneity.
5.2 Transitory Idiosyncratic Shocks

To derive a measure of transitory demand shocks, we follow the strategy used for the estimation of the demand elasticity $\sigma$. Hence, we use the Solow residual as an instrument for prices in an estimation of a log-linearized version of the demand equation (2), where time dummies control for aggregate shocks and firm fixed effects eliminate between-firm permanent heterogeneity. Since the ensuing residuals of the estimated equation represent changes in sales without price adjustments, they can serve as a measure of demand shocks. This strategy is similar in spirit to the approach followed by Foster, Haltiwanger, and Syverson (2008). Thus, we label these shocks “FHS demand”.

In contrast to the SVAR filter, however, this procedure does not differentiate between permanent and transitory shocks, and the processes do not account for factor price shocks. The correlation between FHS demand and our SVAR demand shocks is 0.538 and the standard deviation is considerably higher for the FHS demand shocks (0.24 versus 0.16). Thus, the two demand-shock series appear to contain a common component without being identical. The correlation with between FHS demand and the factor price component of the SVAR is considerably smaller (−0.25), but statistically significant. As expected, the FHS-demand series is uncorrelated with the SVAR technology shocks. Also as expected, given the limited dynamics observed in the physical Solow residual series, the physical Solow residual is highly correlated with the SVAR-technology shocks (0.98), and only marginally related to SVAR demand (correlation of 0.02) and factor price shocks (correlation of 0.06).

We first estimate the impact on employment of FHS demand and the Solow residual as measures of shocks (see column 2 of Table 6). To facilitate the comparison, estimates with our SVAR shocks are presented in column 1. Although the main message still holds when using the FHS-series (the short-run impact of demand shocks is 10 times that of the technology shock in the short run, and 5 times in the long run) it is also noticeable, that the estimated impact of demand shocks is about half as large when using FHS demand as when using the SVAR demand shock. In contrast, the estimated impact of the technology shock is slightly larger when using the raw Solow residual.

As noted above, FHS demand includes both transitory and permanent shocks, as well as an element of factor price shocks. To ascertain whether the impact of demand shocks differs depending on the time-series properties of the shock, we have extracted
Table 6: Baseline Estimates vs. Solow Residuals and FHS Demand Shocks

<table>
<thead>
<tr>
<th></th>
<th>SHORT RUN</th>
<th></th>
<th>LONG RUN</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>(1)</td>
<td>(2)</td>
<td>(3)</td>
</tr>
<tr>
<td>Baseline Technology ($\eta^a$)</td>
<td>0.153</td>
<td>0.333*</td>
<td>0.504*</td>
<td>0.993**</td>
</tr>
<tr>
<td></td>
<td>(0.159)</td>
<td>(0.168)</td>
<td>(0.214)</td>
<td>(0.250)</td>
</tr>
<tr>
<td>Demand ($\eta^o$)</td>
<td>5.986**</td>
<td>3.406**</td>
<td>6.357**</td>
<td>4.061**</td>
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<tr>
<td></td>
<td>(0.233)</td>
<td>(0.183)</td>
<td>(0.310)</td>
<td>(0.252)</td>
</tr>
<tr>
<td>Observations</td>
<td>40,451</td>
<td>40,451</td>
<td>34,414</td>
<td>34,414</td>
</tr>
<tr>
<td>Firms</td>
<td>6,125</td>
<td>6,125</td>
<td>6,116</td>
<td>6,116</td>
</tr>
</tbody>
</table>

Note: Effect of one s.d. shock. In the FHS column the technology shock is the Solow residual, and the demand shock is FHS demand, as defined in the main text. Robust standard errors in parentheses. Regression includes time dummies and firm fixed effects. Long-run impact is based on the sum of the contemporary effect and the effect of the first lag. Regression sample limited to observations where the absolute value of both the technology and the demand shock is less than or equal to two sd. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.

The transitory demand component of the FHS shock. We run a regression with FHS demand as the dependent variable and the SVAR demand, SVAR technology (although this part is irrelevant in practice) and SVAR factor price shocks as regressors and use the residuals measures of transitory demand shocks. Because this residual is measured in the same units, we can directly compare its impact on employment adjustments with the SVAR demand shock, which represent permanent shocks.\(^{34}\)

In Figure 11, we analyze the impact of transitory shifts in product demand on net employment changes. For comparison, the figure also reproduces the baseline response to a permanent demand shock (as in the right-hand side panel of Figure 5). As before, we allow for second-order polynomials of negative and positive shocks, respectively. The results show that the impact of the transitory shocks is substantially lower than the impact of the permanent shocks.\(^{35}\)

These results mirror those of Guiso et al. (2005), which shows that wages respond

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\(^{34}\) The decomposition resembles Guiso et al. (2005), which extracts the permanent component of firm-level value added using high-order polynomials of lags as instruments. Although the mechanics of the methods differ, the underlying logic is similar. Note, however, that an additional value added from our strategy is that we are able to remove the factor price component. Because the bulk of the technology shock process is persistent enough to show up as permanent in our analysis (as noted in the text, the correlation between the two shocks is 0.98), we do not perform a corresponding analysis for the technology shock.

\(^{35}\) Notably, the effect is even smaller, and insignificant, if we do not remove the factor price shock component.
Figure 11: Net Employment, Permanent and Transitory Demand Shocks

Net Employment Rate

Demand

Transitory Demand

Net Employment Rate

Note: Contemporaneous net employment rate in percentage units as a (non-linear) function of an x sd. of the baseline permanent demand shock and of the transitory demand shock (calculated as the residual component of FHS demand). Shaded areas depict 95 percent confidence intervals.

to permanent shocks but not to transitory shocks, which they interpret as insurance provided by the firm. The results imply that firms’ employment adjustment crucially depends on the time-series properties of the shocks. This is important because the welfare consequences of firms’ lack of adjustment are likely to crucially depend on these properties. Labor hoarding in the face of negative transitory shocks may be welfare-enhancing in the presence of uninsurable labor market risk (Bertola, 2004), whereas the ability of firms to adjust to permanent shocks is likely to be crucial for long-run allocative efficiency.

6 Conclusions

This paper has analyzed how firms adjust their labor inputs in response to permanent idiosyncratic firm-level shocks to technology and demand. We identify the shocks by imposing a set of long-run restrictions in an SVAR estimated on firm-level data. The restrictions are derived from a stylized model of a monopolistically competitive firm. The SVAR is estimated using dynamic panel-data methods, allowing us to identify the parameters of the reduced form with considerable precision. To estimate the model, we rely on a unique data-set that merges information about inputs, outputs, and
prices of Swedish manufacturing firms with a linked employer-employee data-set.

The shocks derived from the SVAR affect output and prices in a theory-consistent way, which lends support to their interpretation as demand and technology disturbances. Firm-level output responds vigorously to both technology and demand shocks. In contrast, firm-level prices fall in response to positive technology shocks, but they remain independent of product demand innovations.

Our labor-adjustment results show that both the nature and the time-series properties of the shocks matter. Permanent demand shocks, which affect output but not relative prices, have a pronounced impact on employment. In line with other recent studies, technology shocks have relatively limited employment effects despite affecting both output and relative prices.

A possible limitation of our study is the focus on the manufacturing sector, the sector for which technology shocks can be reasonably approximated. However, it seems likely that the overwhelming force of idiosyncratic demand shocks as a source of employment adjustments in manufacturing firms should provide a lower bound for the importance of demand within other sectors. Demand is likely to play an even more important role for reallocation in service sectors, where product differentiation (and hence demand shocks) is likely to be even more important than in manufacturing.

We further provide the first analysis of the causal impact of job flows on the composition of worker flows, using our permanent demand shocks as an instrument for adjustments in the number of jobs. The results suggest that employment adjustments in response to permanent shifts in the product demand curve are fast and symmetric. By far the largest part of employment adjustment takes place within a year. Almost as much of the employment adjustments are through changes in the separation rates as through changes in the hiring rates, suggesting that both margins should be considered endogenous at the firm-level. Moreover, there are no signs of non-linear responses in hires or separations. Finally, the sign of the shock determines the primary margin of adjustment: firms primarily adjust through separations if shocks are negative and primarily through hires if shocks are positive.

The speed of adjustment, the symmetry between hires and separations as adjustment margins, and the continued recruitment of workers in the face of negative shocks jointly suggest that labor market rigidities play a very limited role in hampering firm-level labor adjustments in the face of permanent idiosyncratic demand shocks. However, the adjustments with respect to transitory shocks are heavily muted.
firms accommodate the impact of permanent shocks, but hoard labor and refrain from
hiring when hit by transitory shocks.

Overall, our results imply that cross-country comparisons of labor flows need to
be careful in accounting for the types of the shocks that hit these economies, because
responses depend not only on the nature of the shocks (technology versus demand)
but also on the time-series properties of these shocks: Labor market adjustments will
differ depending on the prevalence of permanent versus transitory components within
the shock distribution.

Building on this notion, our empirical approach also suggests a route forward in
trying to understand the forces behind the declining rates of labor adjustments ob-
erved in the United States in particular. Essentially, our empirical approach provides
a tool for assessing whether this development is due to a changing nature of firm-level
shocks or due to a reduced impact of these shocks on labor reallocation. Although this
question is beyond the scope of this paper, it serves as a good example of the questions
that future research can answer by combining data on labor flows and well-identified
firm-level shocks.
References


Appendices - For Online Publication

A Derivation of Long-Run Restrictions

A.1 Baseline Model

We use the stylized model presented in the paper to filter out shocks that permanently shift the firms’ production functions and demand curves. To filter out the shocks of interest, we first note that the assumptions of the model ensure that the only shock that can affect the physical gross output Solow residual \((A)\) is the technology shock. Since we only impose this restriction in the long run, we can allow for temporary variations in factor utilization and inventories.

Further, we use the standard result that a firm’s optimal pricing rule under these conditions is to set the price, \(P_{jt}\), as a constant markup \(\sigma/(\sigma - 1)\) over marginal cost, \(MC_{jt}\). Marginal cost is, in optimum, equal to

\[
MC_{jt} = A_{jt}^{-1} \left( \frac{W_{jt}}{\alpha} \right)^{\alpha} P_{jt}^{F}.
\]

Using (A1) and that \(MC_{jt} = (W_{jt}N_{jt})/(\alpha Y_{jt})\) in optimum to get

\[
(W_{jt}N_{jt}/Y_{jt})W_{jt}^{-\alpha} = \alpha^{1-\alpha} A_{jt}^{-1} P_{jt}^{F}.
\]

Thus, expression (A2) will be affected by technology and factor-price shocks but not demand shocks. It is also worth noting that any direct shocks to the firm-level wage-setting relationship (such as changes in the degree of competition over similar types of labor) will not drive this expression. Essentially, expression (A2) is a measure of unit labor cost \((W_{jt}N_{jt}/Y_{jt})\) net of wage-setting disturbances.\(^{36}\) We therefore refer to the variable as wage-neutral labor cost \((WNULC_{jt})\).

Using the demand equation (2) and expression (A1), we arrive at

\[
Y_{jt} W_{jt}^{\sigma \alpha} = \psi Y_{t} P_{t}^{\sigma} A_{jt}^{\sigma} (P_{jt}^{F})^{-\sigma} \Omega_{jt},
\]

where \(\psi = \left( \frac{1}{\alpha} \right)^{-\sigma \alpha} \left( \frac{\sigma}{\sigma - 1} \right)^{-\sigma}.\) Thus, expression (A3) will be driven by shocks to technology, factor prices other than labor, and demand (apart from aggregate factors that

\(^{36}\)Note also that unit labor cost is proportional to marginal cost.
will be captured by time dummies in the empirical implementation of the model). In effect, expression (A3) is demand adjusted for wage-setting disturbances. Thus, we refer to it as wage-neutral demand \( W^{ND}_{jt} \) in the text.

### A.2 Identification of Structural Parameters from Impulse Responses

In this appendix section we show that the three identifying long-run restrictions can be reconciled with our observed impulse responses. As shown in the paper, the theoretical long-run predictions for the response of prices, output and employment to technology and demand shocks under the constant-\( \sigma \) assumption are given by

\[
J^T = \begin{bmatrix}
\frac{\partial \ln P_{jt}}{\partial \ln A_{jt}} & \frac{\partial \ln P_{jt}}{\partial \ln Y_{jt}} \\
\frac{\partial \ln A_{jt}}{\partial \ln Y_{jt}} & \frac{\partial \ln A_{jt}}{\partial \ln Y_{jt}} \\
\frac{\partial \ln N_{jt}}{\partial \ln Y_{jt}} & \frac{\partial \ln \Omega_{jt}}{\partial \ln Y_{jt}} \\
\frac{\partial \ln A_{jt}}{\partial \ln \Omega_{jt}} & \frac{\partial \ln N_{jt}}{\partial \ln \Omega_{jt}}
\end{bmatrix} = \begin{bmatrix}
-1 & 0 \\
\sigma & 1 \\
(\sigma - 1) & 1
\end{bmatrix},
\]

which implies a proportionality factor in the employment responses to technology and demand shocks of \( \frac{1}{\sigma - 1} \). The corresponding empirical Jacobian, derived from the implied elasticities associated with the impulse responses presented in Figures 1 and 2 in the paper, is

\[
J^E = \begin{bmatrix}
-0.215 & 0.015 \\
0.637 & 0.711 \\
0.050 & 0.393
\end{bmatrix},
\]

with robust standard errors presented in parenthesis. Thus, one may be tempted to use the Jacobians \( J^T \) and \( J^E \) to derive an estimate of the structural parameter \( \sigma \) by either looking directly at the response of output to the technology shock, or by evaluating the relative impact of technology and demand shocks. However, as we note in the text, the constant-\( \sigma \) model is deliberately stylized to facilitate a reduced form identification, and not designed to provide the basis for structural estimation of the parameters of the model. Specifically, since small departures from this original model that retain the same identification restrictions would lead to very different interpretations of the structural parameters. Assuming, as in Section A.2 of the paper, that the elasticity of demand (and thereby the markup) may be affected by technology and demand shocks,
\[ Y_{jt} = \left( \frac{P_{jt}}{P_t} \right)^{-\sigma(A_{jt}, \Omega_{jt})} Y_t \Omega_{jt}, \quad \sigma(A_{jt}, \Omega_{jt}) > 1 \text{ and } \sigma(\bar{A}_{jt}, \bar{\Omega}_{jt}) = \sigma, \]  

(A6)

where a bar denotes an average across firms, long-run restrictions remain the same as those imposed in the baseline model.\(^{37}\) However, moving beyond the constant-\(\sigma\) assumption dramatically changes the structural interpretation of the results, as shown in Section A.2 of the paper we get the following Jacobian

\[
\begin{align*}
J_{T_{\text{Extended}}} = & \begin{pmatrix}
-\sigma'_{A_{jt}} \left( \frac{\sigma'}{\sigma-1} \right) & -\sigma'_{\Omega_{jt}} \\
\frac{\sigma'_{A_{jt}}}{(\sigma-1)} + \sigma & \frac{\sigma'_{\Omega_{jt}}}{(\sigma-1)} + 1 \\
\frac{\sigma'_{A_{jt}}}{(\sigma-1)} + \sigma - 1 & \frac{\sigma'_{\Omega_{jt}}}{(\sigma-1)} + 1
\end{pmatrix},
\end{align*}
\]

(A7)

where \(\sigma'_{A_{jt}}\) and \(\sigma'_{\Omega_{jt}}\) denote the derivatives of \(\sigma(A_{jt}, \Omega_{jt})\) with respect to \(A_{jt}\) and \(\Omega_{jt}\), respectively. Interestingly, imposing \(\sigma = 3.306\) (as is the baseline in the paper) and minimizing a loss function (akin to how overidentification is handled in Generalized Method of Moments estimation) in terms of the sum of the squares of the six elements of \([J_{T_{\text{Extended}}} - J^E]\), weighted by the inverse of the standard deviation of the respective element in \(J^E\), with respect to \(\sigma'_{A_{jt}}\) and \(\sigma'_{\Omega_{jt}}\), yields \(\sigma'_{A_{jt}} = -5.857\) and \(\sigma'_{\Omega_{jt}} = -0.763\). The implied reduction in \(\sigma\) from a 1 standard deviation technology shock is moderate (calculated as the derivative times the standard deviation, i.e. \(-5.857 \times 0.101 = -0.592\) ) and even smaller in the case of a demand shock \((-0.763 \times 0.162 = -0.124\) ). In fact, both are tiny compared to the variations of \(\sigma\) (from 1.1 to 10) considered in the main text as robustness exercises. Interestingly, the effect on the markup from a technology (demand) shock equals \(-1/(1-\sigma)^2\) times the derivative \(\sigma'_{A_{jt}}\) (\(\sigma'_{\Omega_{jt}}\)), which implies that the firm increases the markup slightly in response to a 1 standard deviation technology shock, 0.111 whereas the markup response to a 1 standard deviation demand shock is very small (0.023). These results are thus in line with the standard “smoothed-off kinked” demand-curve interpretation suggested by Kimball (1995). More importantly, computing the elements in \(J_{T_{\text{Extended}}}^{\text{Extended}}\) using \(\sigma = 3.306\), \(\sigma'_{A_{jt}} = -5.857\) and \(\sigma'_{\Omega_{jt}} = -0.763\) gives

\(^{37}\)Moreover, as discussed in the main text, our estimation strategy provide employment responses to technology and demand shocks that are insensitive to large variations in estimated values of \(\sigma\). Thus, treating \(\sigma\) as constant or not will be irrelevant for the main results for all reasonable variations in \(\sigma\).
which is well in line with the estimated responses of prices, output and employment to the two shocks \( (J^E) \). It should be noted that alternative permutations of the original model may be consistent with the results. The main point of this exercise is to show that the identifying assumptions we rely on are consistent with the responses we observe. Obviously, it would be straightforward to decrease the distance for any particular (set of) element(s) within the matrix by giving it a higher relative weight when minimizing the loss function.

A.3 Non-Constant Returns to Scale

The model can be easily extended to accommodate non-constant returns to scale. Define the overall returns to scale as \( \lambda = \alpha + \beta + \gamma \). Notice that under non-constant returns to scale, it is straightforward to show that the measurement of the variables in the system of equations needs to be changed to those of Table A1 to retain the recursive form of the long-run impact of the structural shocks. Also note that the cost share of a factor will equal the output elasticity divided by the overall returns to scale in optimum, which we use in the empirical implementation provided in columns 2 and 3 of Table 3 in the main text.

<table>
<thead>
<tr>
<th>Table A1: Summary of Structural System (Non-Constant Returns)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Variables:</strong></td>
</tr>
<tr>
<td>Solow:</td>
</tr>
<tr>
<td>WNULC:</td>
</tr>
<tr>
<td>WND:</td>
</tr>
</tbody>
</table>

B Data

The firm data-set we use is primarily drawn from Sweden’s Industry Statistics Survey (IS) and contains annual information for the years 1990–2002 on inputs and output for.
all Swedish manufacturing plants with 10 employees or more and a sample of smaller plants. Here we focus on firms that have at least 10 employees and that we observe in a spell with at least five observations (the minimum panel dimension required for the SVAR to pass diagnostic tests).

Our measure of real output, \( Y_{jt} \), is the value of total sales taken from the IS deflated by a firm-specific producer-price index. The firm-specific price index is a chained index with Paasche-type links that combines plant-specific unit values and detailed disaggregated producer-price indices (either at the goods level, when available, or at the most disaggregated sectoral level available). Note that when a plant-specific unit-value price is missing (e.g., when the firm introduces a new good), Statistics Sweden tries to find a price index for similar goods defined at the minimal level of aggregation (starting at four-digit goods-code level). The disaggregated sectoral producer-price indices are only used when a plausible goods-price index is unavailable.

To compute the input index \( \Delta z_{jt} \), which is necessary for the computation of the Solow residual \( \Delta a_{jt} \), real intermediate inputs \( M_{jt} \) are measured as the sum of costs for intermediate goods and services (including energy) collected from the IS deflated by a three-digit (SNI92/NACE) producer-price index collected by Statistics Sweden. The real capital stock \( K_{jt} \) is computed using a variation of the perpetual inventory method. In the first step, we calculate the forward recursion

\[
K_{jt} = \max((1 - \delta)K_{j(t-1)} + I_{jt}, BookValue_{jt}), \quad (B1)
\]

where \( \delta \) is sector-specific depreciation rate (two-digit SNI92/NACE) and is computed as an asset-share-weighted average between the machinery and buildings depreciation rates (collected from Melander (2009), Table 2); \( I_{jt} \) is real net investments in fixed tangible assets (computed using a two-digit SNI92/NACE sector-specific investment deflator collected from Statistics Sweden); and \( BookValue_{jt} \) is the book value of fixed tangible assets taken from the Firm Statistics data base maintained by Statistics Sweden, deflated using the same deflator as for investment. Moreover, \( K_{j0} \) is set to zero if the initial book value is missing in the data. Since, for tax reasons, the firms want to keep the book values low, we use the book values as a lower bound of the capital stock. In a second step, we then calculate the backward recursion

\[
K_{j(t-1)} = \frac{K_{jt} - I_{jt}}{(1 - \delta)}, \quad (B2)
\]
where the ending point of the first recursion, \( K_{JT} \), is used as the starting point for the second backward recursion. This is done to maximize the quality of the capital-stock series given that we lack a perfectly reliable starting point and the time dimension is small. The labor input (i.e., number of employees) is taken from the IS. To compute the cost shares, we also need a measure of the firms’ labor cost, which is defined as total labor cost (including payroll taxes) in the IS.

When computing \( \Delta a_{jt} \), we take an approach akin to the strategy outlined by Basu, Fernald, and Shapiro (2001). Thus, the \( C_J \) (i.e., the output elasticities) are treated as constants. Second, the cost shares are estimated as the time average of the cost shares for the two-digit industry to which the firm belongs (SNI92/NACE).\(^{38}\) Third, to calculate the cost shares, we take total costs as approximately equal to total revenues.\(^{39}\) The cost share of capital is then given by one minus the sum of the cost shares for all other factors.

Since 1996, Statistics Sweden has imputed the allocation of production across different plants within multi-plant firms. For this reason, we have explored various cuts of the data either focusing on single-plant firms throughout or use multi-plant firms before 1996 but only single-plant firms thereafter. The results are shown in Table D2 in Appendix D and discussed in the robustness section of the paper.

When computing \( \Delta \text{wnulc}_{jt} \) and \( \Delta \text{wnd}_{jt} \), we use \( C_N \) as the estimate of \( \alpha \) and the measure of the firms’ labor costs together with the measure of real output and labor input (all discussed above). Also, when computing \( \Delta \text{wnd}_{jt} \), we set \( \sigma \) equal to our estimate of 3.306. Finally, we remove 2 percent of the observations in each tail for each of the distributions of \( \Delta a_{jt} \), \( \Delta \text{wnulc}_{jt} \), \( \Delta \text{wnd}_{jt} \), and \( \Delta y_{jt} \). This has little effect on estimated coefficients, but it ensures that the SVAR passes diagnostic tests. We finally require the firm to be observed in spells of at least five years (because we are interested in the within-firm dynamics when estimating the SVAR).

In the end, we construct series for \( \Delta a_{jt} \), \( \Delta \text{wnulc}_{jt} \), \( \Delta \text{wnd}_{jt} \), and \( \Delta y_{jt} \) for 7,940 ongoing firms (observed at least during five consecutive years), over the 1991 – 2002

---

\(^{38}\) In the calculation we drop firm/year observations in which the (residual) capital share is below –25 percent of sales. This procedure generates reasonable aggregate cost shares, and ensures that the cost shares in all industries are positive.

\(^{39}\) Using the data underlying Carlsson (2003), and relying on a no-arbitrage condition from neoclassical investment theory (also taking the tax system into account) to calculate the user cost of capital, we find that the time average (1968 – 1993) for the share of economic profits in aggregate Swedish manufacturing revenues is about –0.001, thus supporting the the approximation of cost shares by revenue shares. The result of approximately zero economic profits on average is similar to findings in U.S. data; See e.g. Basu, Fernald, and Shapiro (2001) for a discussion.
period. All in all, this amounts to 70,077 firm/year observations. Removing extreme
tail events reduces the sample to 6,137 firms and 53,379 firm/year observations (in
the specification with output growth as the fourth variable). For these firms we
can compute the structural shocks for 41,105 firm/years (due to lags in the model).
Finally, we can match on labor flows from RAMS for 6,125 firms and 40,451 firm/year
observations. Note that the procedure outlined above implies that changing the fourth
variable in the VAR introduces small changes in the sample size.

C  The SVAR

C.1  Identification

The model outlined in the paper and presented in detail in Appendix A provides
a set of three equations that depend on the three structural shocks (i.e., demand,
technology, and intermediate inputs). The left-hand-side variables in these equations
can all be constructed from our firm-level data, and the model motivates a recursive
sequence of long-run restrictions regarding the impact of the structural shocks on
these variables. To extract the shocks of interest from the system, we estimate a VAR
and proceed along the lines of Blanchard and Quah (1989).

Since we are interested in how other variables (such as output, prices, and em-
ployment) respond to structural shocks, we start by including these other variables
as fourth variables in the system, allowing each to have a long-run effect on itself but
not on the other variables in the system. These variables will thus also soak up all
remaining transitory dynamics. In practice, we rotate across these variables while
keeping the core system of the first three equations intact as in Ramey (2011). Parts
of our analysis rely on extracting the technology and demand shocks from the system.
In these exercises we use output as the fourth variable, but we also present several
robustness checks showing that the results are insensitive to this choice. The VAR
system, a fully interacted dynamic system of the variables, can, under standard regu-
ularity conditions, be written in a vector moving average (MA) form. Using lowercase
letters for logarithms and denoting the fourth variable by \( \theta \), the MA representation
of the system follows:\(^{40}\)

\[^{40}\text{Note that the assumed functional form of the processes for demand and technology shifters specified in equations (3) and (4) directly leads to equation (C1).}\]
We assume that the shocks \([\eta^0_{jt}, \eta^f_{jt}, \eta^o_{jt}, \eta^h_{jt}]\) are structural innovations and hence mutually orthogonal and serially uncorrelated. Because the shock associated with the fourth variable lacks a theoretical interpretation, we refer to it as the “residual” shock in what follows. The terms \(C_{rc}(L)\) are polynomials in the lag operator, \(L\), with coefficients \(c_{rc}(k)L^k\) at each lag \(k\). The shocks are orthogonal, and using a standard normalization we get \(E \eta_t \hat{\eta}_t = I_t\), where \(\eta_t = [\eta^0_{jt}, \eta^f_{jt}, \eta^o_{jt}, \eta^h_{jt}]’\).

Following standard practice, we denote the elements of the matrix of long-run multipliers corresponding to \((C1)\) as \(C_{rc}(1)\). Relying on the model outlined above, we know that the technology shock, \(\eta^0_{jt}\), is the only shock with a long-run impact on \(a_{jt}\), so \(C_{12}(1) = C_{13}(1) = C_{14}(1) = 0\) in the matrix of long-run multipliers.\(^{41}\) Similarly, only the technology and the factor-price shocks have a long-run effect on \(wnulc_{jt}\), so \(C_{23}(1) = C_{24}(1) = 0\). Finally, since the residual shock has no long-run effects on wage-neutral demand, it follows that \(C_{34}(1) = 0\).

Given these assumptions, we can recover the time series of the firm’s structural shocks \(\eta_{jt}\) from an estimate of the VAR\((p)\) formulation of the system \((C1)\), i.e., from

\[
\Delta x_t = \sum_{i=1}^{P} A_p \Delta x_{t-p} + e_t, \tag{C2}
\]

where \(A_p\) denotes the matrices with coefficients, \(\Delta x_t = [\Delta a_{jt}, \Delta wnulc_{jt}, \Delta wnd_{jt}, \Delta \theta_{jt}]’\), \(e_t\) is a vector of reduced-form disturbances, and we have suppressed constants to save on notation.

Under standard regularity conditions, there exists a VAR representation of the MA representation \((C1)\) of the form

\[
x_t = A(L)x_{t} + e_t, \tag{C3}
\]

where \(x_t = [\Delta a_{jt}, \Delta wnulc_{jt}, \Delta wnd_{jt}, \Delta \theta_{jt}]\), \(A_{rc}(L) = \sum_{k=0}^{\infty} a_{rc}(k)L^k\) and \(e_t\) is a vector of reduced-form errors. Since the errors in the VAR, \(e_t\), are one-step-ahead forecast

\(^{41}\)That is, the coefficients \(c_{12}(k)\) are such that \(\sum_{k=0}^{\infty} c_{12}(k) = 0\), and similarly for the coefficients \(c_{13}(k)\) and \(c_{14}(k)\).
errors, we will have that
\[ \mathbf{e}_t = \mathbf{c}(0) \mathbf{\eta}_t, \]
(C4)
where \( \mathbf{c}(0) \) is the matrix of \( c_{rc}(0) \) coefficients from the MA representation and \( \mathbf{\eta}_t = [\eta_{jt}^0, \eta_{jt}', \eta_{jt}'', \eta_{jt}'''\prime]' \). Thus, if the 16 coefficients in \( \mathbf{c}(0) \) were known, we could recover \( \mathbf{\eta}_t \).

In practice, we first use that \( \mathbf{E} \mathbf{\eta}_t \mathbf{\eta}_t' = \mathbf{I} \), together with an estimate of \( \mathbf{\Omega} = \mathbf{E} \mathbf{e}_t \mathbf{e}_t' \), from our estimates of equation (C3) to obtain 10 restrictions. In addition, we impose the 6 long-run restrictions. Finally, rewriting equation (C3), we can obtain the MA form by using equation (C4) in terms of coefficients from equation (C3) and the \( \mathbf{c}(0) \) coefficients as
\[ \mathbf{x}_t = [\mathbf{I} - \mathbf{A}(L)\mathbf{L}]^{-1} \mathbf{c}(0) \mathbf{\eta}_t. \]
(C5)
Then, our 6 long-run restrictions imply an equal number of restrictions on the matrix \([\mathbf{I} - \mathbf{A}(L)\mathbf{L}]^{-1} \mathbf{c}(0)\), that together with an estimate of (C3) yields 6 additional restrictions on \( \mathbf{c}(0) \). Jointly, these 16 restrictions provide an estimate of the \( \mathbf{c}(0) \) matrix, \( \hat{\mathbf{c}}(0) \), and using these we can solve for the structural shocks using equation (C4):
\[ \hat{\mathbf{c}}(0)^{-1} \mathbf{e}_t = \hat{\mathbf{\eta}}_t. \]
(C6)

When deriving results in term of elasticities, and to obtain an estimate of the standard deviation of the structural shocks, we use a re-normalized \( \hat{\mathbf{c}}(0) \) where each element is divided by its column diagonal element.

C.2 Impulse Responses, Variance Decompositions, and Tests

Relying on the Arellano and Bond (1991) autocorrelation test of the differenced residual, two lags in the VAR are enough to remove any autocorrelation in the residuals in all four equations. Here we rely on the two-step Arellano and Bond (1991) difference estimator, using the second to the fourth lag levels as instruments. It is worth noting, though, that the parameter estimates are not sensitive to the actual choice of where to cut the instrument set. The results are also insensitive to the inclusion of more lags as instruments. As an additional precaution, we collapse the instrument set to avoid overfitting. That is, we impose the restriction that the relationships in the “first stage” are the same across all time periods (see Roodman, 2006, for a discussion). For all specifications, the Hansen test of the overidentifying restrictions cannot reject the null of a correct specification and valid instruments.
Figure C1: Impulse Responses

Impulse Responses to a Technology Shock

Impulse Responses to a Factor-Price Shock

Impulse Responses to a Demand Shock

Impulse Responses to a Residual Shock

Note: Impulse responses of the Solow residual, wage neutral unit labor costs (wage neutral ULC), wage-neutral demand and output in the baseline VAR to a 1 sd. shock in percentage points. Each line depicts the mean of the bootstrap distributions. Shaded areas depict the bootstrapped 95 percent confidence intervals calculated from 1,000 replications.
Figure C2: Variance Decompositions

Note: Forecast-error variance decompositions of the VAR in levels. W-N Demand denotes wage-neutral demand. W-N ULC denotes wage-neutral unit labor costs. The left-most panel shows the percentage of the forecast-error variance in the Solow residual that can be explained by each structural shock at different horizons. Each line depicts the mean of the bootstrap distributions. Shaded areas depict the bootstrapped 95 percent confidence intervals calculated from 1,000 replications.
Figure C3: The Distribution of Demand and Technology Shocks

Note: Histograms of demand and technology shocks. Distributions normalized to have unit standard deviation. Dashed lines depict a normal distribution.

Figure C1 shows the impulse responses of each of the variables in the baseline VAR in levels to each of the structural shocks. Since the estimated system converges fairly rapidly, we only plot the initial five periods. All impulse responses are precisely estimated as indicated by the tight (95 percent) confidence bands based on 1,000 bootstrap replications. The high level of precision is not surprising, given that we estimate the impulse responses on a much larger sample than is common in macroeconomic applications.

Unfortunately, we have not been able to find any statistical tests of stationarity that are suitable for a setting with a short but wide panel. However, it should be clear from Figure C1 that this issue is of little importance in the current setting. Importantly, the figure is expressed in log-levels, and the flat, non-zero-end-segments in the responses imply that shocks do have permanent effects on the levels of the series (i.e., the levels are $I(1)$) and that the differenced series are stationary ($I(0)$).

The first row of Figure C1 traces out the impulse responses of the Solow residual, the $wnulc$, the $wnd$, and output to a 1 sd. technology shock, $\eta_{jt}$. Technology shocks have a positive permanent effect on the Solow residual: a “normal” (i.e., 1 sd) shock increases the Solow residual slightly less than 10 percent in the long run. The estimated VAR model does not impose any restrictions on how technology shocks affect
Figure C4: Non-Linear Responses to a Technology Shock

Note: Contemporaneous response of variables included in the baseline VAR in percentage units as a (non-linear) function of an x sd. technology or demand shock. Shaded areas depict the 95 percent confidence intervals.
However, the results do concur with predictions from expression (A2) in the sense that \(\text{wnulc}\) falls permanently in response to the (permanent) technology shock. Similarly, we find that a permanent technology shock raises \(\text{wnd}\), as predicted from expression (A3).

The second row in Figure C1 reports the impulse responses to a 1 sd. permanent factor-price shock. A “normal” factor-price shock increases \(\text{wnulc}\) and lowers \(\text{wnd}\) permanently (theoretically working through marginal cost, price setting, and demand). The latter result is, again, an unconstrained result in line with predictions from expression (A2). By the same logic, output also falls permanently in response to a factor-price shock. The Solow residual is affected in the very short run by factor-price shocks but converges to the long-run restriction fairly rapidly.

The impulse responses to a permanent demand shock are shown in the third row of Figure C1. In this case, \(\text{wnd}\) is permanently increased in response to a permanent demand shock. In the short run, demand shocks increase the Solow residual and reduce \(\text{wnulc}\). As expected, a demand shock also has permanently positive effects on output. A “normal” demand shock increases it by about 10 percent in the long run. For completeness, Figure C1 also reports the responses to the residual shock in the last row. A “normal” residual shock raises output permanently by slightly more than 5 percent.

Figure C2 presents forecast error variance decompositions for each of the variables in the VAR in levels, decomposing the movements of the three variables. Again, bootstrapped confidence bands are extremely tight. Quantitatively, the Solow residual is solely driven by technology shocks on all horizons. The \(\text{wnulc}\) is mostly driven by factor-price shocks (75 percent of the variation) and partly by technology shocks (25 percent). Demand shocks explain about 65 percent of the movements in \(\text{wnd}\), whereas factor-price shocks explain about 20 percent. We also see in Figure C2 that there is a role for technology shocks in explaining wage-neutral demand movements, accounting for about 15 percent. For output, we see that about 55 percent of the variation is driven by demand shocks, the rest being explained by factor-price shocks (about 20 percent), technology (about 15 percent), and the transitory shock (about 10 percent).

Overall though, we find the residual shock to be of little importance. Given that we include time dummies in the VAR, this finding is in line with the results of Franco and Philippon (2007), which finds that transitory shocks are not very important on
the firm level but account for most of the volatility of aggregates because they are correlated across firms.

Figure C3 shows the distributions for extracted innovations to technology and demand. As the two panels of the figure show, neither the demand nor the technology shock distributions are particularly skewed (skewness coefficients of $-0.02$ and $-0.14$, respectively), whereas both are leptokurtic (kurtosis coefficients of 5.85 and 4.25). This is also clearly visible in the graphs where the dashed line depicts a normal distribution, and a standard skewness/kurtosis test (D’Agostino, Belanger, and D’Agostino, 1990) rejects the null of normality for both distributions (p-value of 0.00 in both cases). The shock distributions depicted in Figure C3 are normalized to have a unit standard deviation. When re-normalizing the system (see Appendix A), we find that the standard deviation of the demand shock is about 35 percent larger than the technology shock (standard deviations of 16.02 and 11.86 percentage points, respectively).

A maintained assumption in the analysis is that the baseline VAR is linear in the structural shocks. In Figure C4 we plot the predicted contemporaneous responses of the variables included in the VAR as (possibly non-linear) functions of structural shocks (allowing for a separate second-order polynomial above and below zero). As the graphs show, the results do support the maintained linearity assumption.
Table D1: Contemporaneous and Long-Run Effect on Log Employment - Different Values of $\sigma$ and Sectoral Dynamics

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
<th>(5)</th>
<th>(6)</th>
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<tbody>
<tr>
<td></td>
<td>Baseline</td>
<td>$\sigma = 1.1$</td>
<td>$\sigma = 10$</td>
<td>$\sigma$ by sector</td>
<td>$\sigma$ by sector</td>
<td>Sectoral Dynamics</td>
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<tr>
<td></td>
<td>$(\sigma = 3.3)$</td>
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<td></td>
<td></td>
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<tr>
<td><strong>SHORT RUN</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\eta^\alpha$</td>
<td>0.153</td>
<td>0.207</td>
<td>0.259</td>
<td>0.192</td>
<td>0.147</td>
<td>0.126</td>
</tr>
<tr>
<td></td>
<td>(0.159)</td>
<td>(0.158)</td>
<td>(0.152)</td>
<td>(0.161)</td>
<td>(0.162)</td>
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<tr>
<td>$\eta^\omega$</td>
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<td>6.591**</td>
<td>4.060**</td>
<td>5.693**</td>
<td>5.520**</td>
<td>5.506**</td>
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<tr>
<td></td>
<td>(0.233)</td>
<td>(0.240)</td>
<td>(0.198)</td>
<td>(0.221)</td>
<td>(0.222)</td>
<td>(0.225)</td>
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<td>39,207</td>
<td>40,214</td>
<td>39,580</td>
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<td>5,998</td>
<td>6,102</td>
<td>5,997</td>
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<td></td>
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<tr>
<td>$\eta^\alpha$</td>
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<td>0.512*</td>
<td>0.643**</td>
<td>0.599**</td>
<td>0.510*</td>
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<td>(0.214)</td>
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<tr>
<td>$\eta^\omega$</td>
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</tbody>
</table>

Note: Columns (2) and (3) impose large variation in values of $\sigma$. Column (4), (5) and (6) allow for a sectoral $\sigma$ (for sufficiently large two-digit industries). Column (4) retains joint time dummies. Column (5) lets the time dummies be sector specific. Column (6) reestimates the entire SVAR for each two-digit industry. All estimates are the effect of a 1 sd. shock. Robust standard errors in parentheses. Long-run estimates are the sum of the contemporaneous impact and one lag. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.
Table D2: Contemporaneous and Long-Run Effect on Log Employment - Sample Variations

<table>
<thead>
<tr>
<th>Sample</th>
<th>(1) Baseline</th>
<th>(2) Single Plant Always</th>
<th>(3) Single Plant After 1996</th>
<th>(4) ≤ ±2 Sd. Shocks</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>SHORT RUN</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \eta^a )</td>
<td>0.153</td>
<td>0.421**</td>
<td>0.312*</td>
<td>0.040</td>
</tr>
<tr>
<td></td>
<td>(0.159)</td>
<td>(0.158)</td>
<td>(0.151)</td>
<td>(0.164)</td>
</tr>
<tr>
<td>( \eta^\omega )</td>
<td>5.986**</td>
<td>5.500**</td>
<td>6.244**</td>
<td>6.317**</td>
</tr>
<tr>
<td></td>
<td>(0.233)</td>
<td>(0.236)</td>
<td>(0.238)</td>
<td>(0.205)</td>
</tr>
<tr>
<td>Observations</td>
<td>40,451</td>
<td>20,877</td>
<td>30,234</td>
<td>36,072</td>
</tr>
<tr>
<td>Firms</td>
<td>6,125</td>
<td>3,246</td>
<td>5,259</td>
<td>6,111</td>
</tr>
</tbody>
</table>

| **LONG RUN**            |              |                         |                            |                     |
| \( \eta^a \)            | 0.504*       | 0.534*                  | 0.669**                    | 0.336               |
|                         | (0.214)      | (0.233)                 | (0.215)                    | (0.234)             |
| \( \eta^\omega \)       | 6.357**      | 5.715**                 | 6.657**                    | 6.397**             |
|                         | (0.310)      | (0.309)                 | (0.326)                    | (0.294)             |
| Observations            | 34,414       | 17,638                  | 25,040                     | 30,693              |
| Firms                   | 6,116        | 3,246                   | 5,250                      | 6,066               |
| sd. \( \eta^a \)       | 10.06        | 9.13                    | 9.41                       | 10.06               |
| sd. \( \eta^\omega \)  | 16.18        | 15.07                   | 14.79                      | 16.18               |

Note: Column (2) restricts the sample to single-plant firms; column (3) includes a mixed sample with multi-plant firms until 1996, but not thereafter; column (4) shows results for a trimmed sample where we focus on shocks in the Lester range of ±2 standard deviations. Estimates are the effects of a 1 sd. shock. Robust standard errors in parentheses. Regression includes firm fixed effects and time dummies. Long-run estimates are the sum of the contemporaneous impact and one lag. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.
Table D3: Contemporaneous and Long-Run Effect on Log Employment - Varying the Fourth Variable in the VAR

<table>
<thead>
<tr>
<th>Fourth Variable of VAR:</th>
<th>(1) Output</th>
<th>(2) Sales per Worker</th>
<th>(3) Employment (IS)</th>
<th>(4) Employment (RAMS)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**SHORT RUN**

<table>
<thead>
<tr>
<th>Varies</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \eta^a )</td>
<td>0.153</td>
<td>0.524**</td>
<td>0.263</td>
<td>0.499**</td>
</tr>
<tr>
<td></td>
<td>(0.159)</td>
<td>(0.154)</td>
<td>(0.143)</td>
<td>(0.061)</td>
</tr>
<tr>
<td>( \eta^\omega )</td>
<td>5.986**</td>
<td>5.840**</td>
<td>5.261**</td>
<td>6.986**</td>
</tr>
<tr>
<td></td>
<td>(0.233)</td>
<td>(0.234)</td>
<td>(0.212)</td>
<td>(0.086)</td>
</tr>
</tbody>
</table>

Observations: 41,105; 40,284; 38,213; 37,234
Firms: 6,125; 6,113; 5,879; 5,703

**LONG RUN**

<table>
<thead>
<tr>
<th>Varies</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \eta^a )</td>
<td>0.504*</td>
<td>0.812**</td>
<td>0.644**</td>
<td>0.643**</td>
</tr>
<tr>
<td></td>
<td>(0.214)</td>
<td>(0.218)</td>
<td>(0.209)</td>
<td>(0.097)</td>
</tr>
<tr>
<td>( \eta^\omega )</td>
<td>6.357**</td>
<td>6.134**</td>
<td>5.477**</td>
<td>7.514**</td>
</tr>
<tr>
<td></td>
<td>(0.310)</td>
<td>(0.317)</td>
<td>(0.266)</td>
<td>(0.121)</td>
</tr>
</tbody>
</table>

Observations: 34,414; 34,260; 32,407; 31,531
Firms: 6,116; 6,102; 5,871; 5,703

sd. \( \eta^a \): 10.06; 9.980; 9.971; 9.964
sd. \( \eta^\omega \): 16.18; 16.39; 15.35; 15.13

Note: Column (2) derives shocks from a VAR in which the fourth variable is sales per worker; in column (3) the fourth variable is annual employment measured in the IS data set; in column (4) the fourth variable is end-of-the-year employment measured from the RAMS data-set. All estimates are the effect of a 1 sd. shock. Robust standard errors in parentheses. All regressions include time dummies and firm fixed effects. Long-run estimates are the sum of the contemporaneous impact and one lag. ** and * denote statistical significance at the 1 and 5 percent levels, respectively.
Table D4: Contemporaneous and Long-Run Effect on Net Employment Growth - Two Period Specifications.

<table>
<thead>
<tr>
<th></th>
<th>(1) One Period – Baseline</th>
<th>(2) Two Period – Without Exits</th>
<th>(3) Two Period – With Exits</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>SHORT RUN</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \eta^{\alpha} )</td>
<td>0.115</td>
<td>0.328*</td>
<td>0.278</td>
</tr>
<tr>
<td></td>
<td>(0.119)</td>
<td>(0.153)</td>
<td>(0.164)</td>
</tr>
<tr>
<td>( \eta^{\omega} )</td>
<td>5.609**</td>
<td>5.431**</td>
<td>5.749**</td>
</tr>
<tr>
<td></td>
<td>(0.173)</td>
<td>(0.375)</td>
<td>(0.376)</td>
</tr>
<tr>
<td>Observations</td>
<td>40,451</td>
<td>39,822</td>
<td>40,238</td>
</tr>
<tr>
<td>Firms</td>
<td>6,125</td>
<td>6,114</td>
<td>6,121</td>
</tr>
<tr>
<td><strong>LONG RUN</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( \eta^{\alpha} )</td>
<td>0.412*</td>
<td>0.420</td>
<td>0.380</td>
</tr>
<tr>
<td></td>
<td>(0.163)</td>
<td>(0.350)</td>
<td>(0.368)</td>
</tr>
<tr>
<td>( \eta^{\omega} )</td>
<td>6.009**</td>
<td>4.112**</td>
<td>4.696**</td>
</tr>
<tr>
<td></td>
<td>(0.228)</td>
<td>(0.391)</td>
<td>(0.422)</td>
</tr>
<tr>
<td>Observations</td>
<td>34,414</td>
<td>33,830</td>
<td>34,243</td>
</tr>
<tr>
<td>Firms</td>
<td>6,116</td>
<td>6,099</td>
<td>6,110</td>
</tr>
</tbody>
</table>

Note: The dependent variable in column (1) is the employment change between \( t \) and \( t - 1 \) divided by the average employment in the two years. In columns (2) and (3) the dependent variable is defined as the employment change between \( t + 1 \) and \( t - 1 \) divided by the average employment in the two years. Columns (1) and (2) exclude firms that exit the sample in the calculation of the flows, and column (3) includes them. The reported coefficients are the effect of 1 sd. shock. Robust standard errors in parentheses. Regression includes firm fixed effects and time dummies. Long-run estimates are the sum of the contemporaneous impact and one lag. ** and * denote statistical significance at the 1 and 5 levels, respectively.